

Hierarchical Heuristic Species Delimitation Under the Multispecies Coalescent Model with Migration

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Abstract.—The multispecies coalescent (MSC) model accommodates genealogical fluctuations across the genome and provides a natural framework for comparative analysis of genomic sequence data from closely related species to infer the history of species divergence and gene flow. Given a set of populations, hypotheses of species delimitation (and species phylogeny) may be formulated as instances of MSC models (e.g., MSC for 1 species versus MSC for 2 species) and compared using Bayesian model selection. This approach, implemented in the program *BPP*, has been found to be prone to over-splitting. Alternatively, heuristic criteria based on population parameters (such as population split times, population sizes, and migration rates) estimated from genomic data may be used to delimit species. Here, we develop hierarchical merge and split algorithms for heuristic species delimitation based on the genealogical divergence index (*gdi*) and implement them in a Python pipeline called *hmsd*. We characterize the behavior of the *gdi* under a few simple scenarios of gene flow. We apply the new approaches to a dataset simulated under a model of isolation by distance as well as 3 empirical datasets. Our tests suggest that the new approaches produced sensible results and were less prone to oversplitting. We discuss possible strategies for accommodating paraphyletic species in the hierarchical algorithm, as well as the challenges of species delimitation based on heuristic criteria. [BPP; genealogical divergence index; gene flow; giraffes; milksnakes; multispecies coalescent; species delimitation; sunfish.]

Delineation of species boundaries is important for characterizing patterns of biological diversity and guiding conservation policy and practice, particularly during the current global changes in climate and environment. Traditionally, species were identified and distinguished using morphological characteristics. The value of genetic data to species delimitation and identification has long been recognized (e.g., Bateson 1909) as genetic data are informative about many related processes, such as species/population divergence and interspecific hybridization (Fujita et al. 2012). Early methods that use genetic data to identify and delimit species relied on simple genetic-distance cutoffs (such as the “4×” or “10×” rules), requiring interspecific divergence to be a few times greater than intraspecific diversity (Hebert et al. 2003, 2004), or reciprocal monophyly in gene trees (Baum and Shaw 1995) (see, e.g., Sites and Marshall 2003 for a review). However, such criteria may be too simplistic as they do not accommodate polymorphism in ancestral populations and incomplete lineage sorting (Hudson and Turelli 2003) or uncertainties in gene-tree reconstruction (Knowles and Carstens 2007; Yang and Rannala 2017).

While genetic and genomic data are clearly informative concerning the species status of populations, interpretation of this evidence may require a proper statistical inference framework. The processes of biological reproduction and accumulation of mutations in

the sequences are highly stochastic, as are the sampling errors due to finite amounts of data. The multispecies coalescent (MSC) model (Rannala and Yang 2003) provides a framework for analysis of genomic sequence data from closely related species or populations to infer the order and timings of species/population divergences. Likelihood-based implementations of the MSC accommodate incomplete lineage sorting and stochastic variation in gene trees (so that reciprocal monophyly is not needed) as well as phylogenetic uncertainties at each locus (so that one does not have to rely on inferred gene trees), making it possible to infer population histories even when there is widespread incomplete lineage sorting and there is very little phylogenetic information at every locus (Xu and Yang 2016; Jiao et al. 2021). The MSC model has also been extended to accommodate gene flow between species or populations, assuming either a major hybridization/introgression event at a particular time point in the MSC-with-introgression (MSC-I) model (Wen and Nakhleh 2018; Zhang et al. 2018; Flouri et al. 2020) or continuous migration over an extended time period in the MSC-with-migration (MSC-M) model (Nielsen and Wakeley 2001; Gronau et al. 2011; Hey et al. 2018; Flouri et al. 2023). As hybridization appears to occur commonly in both plants and animals (e.g., *Arabidopsis*, Arnold et al. 2016; *Anopheles* mosquitoes, Fontaine et al. 2015; *Panthera* cats, Figueiro et al. 2017;

and Hominins, [Nielsen et al. 2017](#)), it may be important to consider explicitly gene flow in species delimitation.

Species Delimitation Through Comparison of MSC Models

Given a set of populations, different species delimitations correspond to different ways of grouping populations into species. Each species delimitation, together with the phylogeny, for the delimited species can be formulated as an instance of the MSC model and fitted to genomic sequence data sampled from the extant species or populations. Competing models of delimitation can thus be compared via Bayesian model selection using posterior model probabilities or Bayes factors ([Yang and Rannala 2010](#); [Ji et al. 2023](#)). In the Bayesian program *BPP*, this is accomplished by using a Markov chain Monte Carlo (MCMC) algorithm to calculate the posterior probabilities for different MSC models ([Yang and Rannala 2010, 2014](#); [Yang 2015](#); [Flouri et al. 2018](#)). In simulations ([Luo et al. 2018](#)), *BPP* showed lower rates of species overestimation and underestimation than the generalized mixed Yule-coalescent method ([Pons et al. 2006](#); [Fujisawa and Barraclough 2013](#)) or the Poisson tree process method ([Zhang et al. 2013](#)). The approach of model selection appears to be particularly effective in identifying sympatric cryptic species. For example, [Ramirez-Reyes et al. \(2020\)](#) identified 13 new species of leaf-toed geckos in a lineage that diverged 30 Ma.

The approach of model selection as implemented in *BPP* has often been noted to identify more lineages as distinct species than many other methods, especially when applied to geographical populations or races ([Sukumaran and Knowles 2017](#)). For example, [Campillo et al. \(2020\)](#) analyzed 99 population pairs in the genus *Drosophila* and found that *BPP* identified 80 pairs as distinct species, whereas reproductive isolation was identified in only 69 pairs. Similarly, [Bamberger et al. \(2022\)](#) studied 48 *Albinaria cretensis* land snail populations, and found that morphological classifications suggested 3–9 species while *BPP* suggested 45–48. [Barley et al. \(2018\)](#) simulated multiple populations from a single species that exhibits population structure and isolation by distance, and found that *BPP* delimited geographically separated populations as distinct species. These studies suggest that the lineages identified by *BPP* sometimes correspond to populations rather than species ([Chambers and Hillis 2020](#)), raising concerns about the apparent over-splitting of *BPP* ([MacGuigan et al. 2021](#)).

Empirical Species Delimitation Based on Population Parameters

Rather than treating species delimitation as a model-selection problem, an alternative approach is to define species status using an empirical criterion based on

parameters that characterize the history of population divergence and gene flow, such as the population split time (T_{AB} , in generations), effective population sizes (N_A, N_B), and migration rates (M_{AB} and M_{BA} , in expected number of migrants per generation). This appears to be a natural approach to take if one recognizes the arbitrariness in species status of allopatric populations. Population parameters can be estimated under the MSC from genomic data, with the stochastic fluctuation of the coalescent process and the phylogenetic uncertainty in genealogical trees accommodated ([Jiao et al. 2021](#)).

[Jackson et al. \(2017\)](#) introduced such a criterion, called the *genealogical divergence index* (*gdi*), by considering the probability that 2 sequences sampled from population *A* (a_1 and a_2) coalesce before either of them coalesces with a sequence (b) sampled from population *B* ([Fig. 1](#)). When a_1 and a_2 coalesce first, the resulting gene tree has the topology $G_1 = ((a_1, a_2), b)$. Let its probability be $P_1 = \mathbb{P}(G_1)$. In the case of no gene flow between *A* and *B*, this is given as

$$P_1 = 1 - \frac{2}{3} e^{-2\tau_{AB}/\theta_A} = 1 - \frac{2}{3} e^{-T_{AB}/2N_A}. \quad (1)$$

The parameter vector is $\Theta = (\tau_{AB}, \theta_A, \theta_B, \theta_{AB})$, with $\tau_{AB} = T_{AB}\mu$ and $\theta_A = 4N_A\mu$, where T_{AB} is the

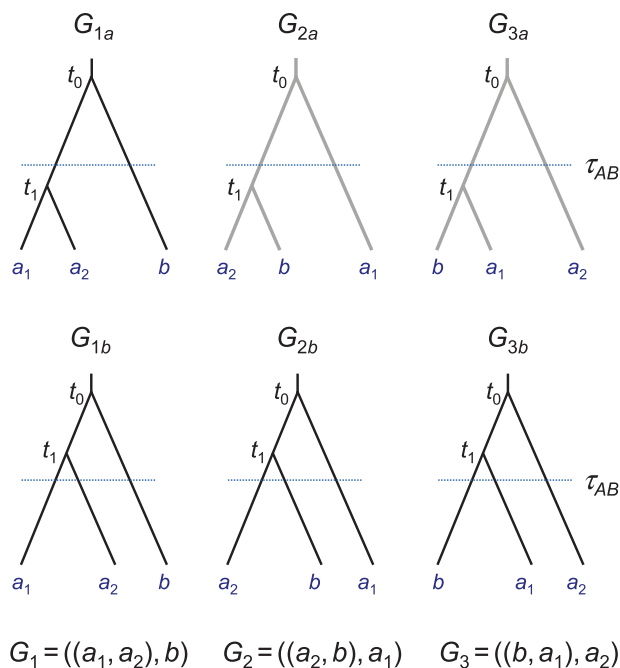


FIGURE 1. Three possible gene trees for a locus with 2 *A* sequences and 1 *B* sequence: $G_1 = ((a_1, a_2), b)$; $G_2 = ((a_2, b), a_1)$; and $G_3 = ((b, a_1), a_2)$. If the first coalescence (occurring at time t_1) is more recent than the population divergence (τ_{AB}), the gene trees are labelled G_{1a} , G_{2a} , and G_{3a} ; otherwise they are labelled G_{1b} , G_{2b} , and G_{3b} . Note that if there is no gene flow between *A* and *B* gene trees G_{2a} and G_{3a} (grayed out) are impossible.

population split time in generations, N_A is the population size of A , and μ is the mutation rate per site per generation. Both τ_{AB} and θ_A are measured in expected number of mutations per site. P_1 is a simple function of $2\tau_{AB}/\theta_A = T_{AB}/(2N_A)$, which is known as branch length in coalescent units since it takes on average $2N_A$ generations for 2 sequences from population A to coalesce. As P_1 ranges from $\frac{1}{3}$ (at $\tau_{AB} = 0$, when populations A and B are at panmixia) to 1 (at $\tau_{AB} \rightarrow \infty$, when A and B are completely isolated), Jackson et al. (2017) rescaled it so that the resulting index ranges from 0 to 1:

$$gdi = \frac{P_1 - \frac{1}{3}}{1 - \frac{1}{3}} = 1 - e^{-2\tau_{AB}/\theta_A} = 1 - e^{-T_{AB}/2N_A}. \quad (2)$$

Based on a meta-analysis of data from Pinho and Hey (2010), Jackson et al. (2017) suggested the rule of thumb that populations A and B should be considered a single species if $gdi < 0.2$, or 2 distinct species if $gdi > 0.7$. Intermediate values ($0.2 < gdi < 0.7$) indicate ambiguous species status. Note that from Equation (2), $gdi = 0.2$ and 0.7 correspond to gene-tree probabilities $\mathbb{P}(G_1) = 0.47$ and 0.8 , respectively, or to split times $T_{AB}/(2N_A) = 0.22$ and 1.20 coalescent units, respectively.

Leaché et al. (2019) described a hierarchical merge algorithm for species delimitation based on gdi . Given a set of populations and a guide tree for them, the procedure attempts to merge, progressively, 2 populations into 1 species, judged by gdi . Here, we develop a python pipeline to automate the procedure, called Hierarchical Heuristic Species Delimitation (HHSd). We include a hierarchical split algorithm as well. The hierarchical procedure of Leaché et al. (2019) relied on the MSC model without gene flow. In our pipeline, we account for gene flow by using the MSC-M model implemented recently in BPP (Flouri et al. 2023).

We first discuss the definition and computation of gdi under the MSC-M model, and then describe the algorithms implemented in HHSd. We examine the behavior of the gdi under several simple models of gene flow. We demonstrate our pipeline by analyzing a dataset simulated under an isolation-by-distance model, both under the MSC model with no gene flow and under the MSC-M model accommodating gene flow. Finally, we apply the pipeline to 3 empirical datasets, for giraffes, milk-snakes, and sunfish and discuss the results in relation to existing delimitations.

THEORY AND METHODS

Redefining the gdi to accommodate complex migration patterns

The definition of Equation (2) works when populations A and B are completely isolated with no gene flow. When A and B exchange migrants, the gene trees can

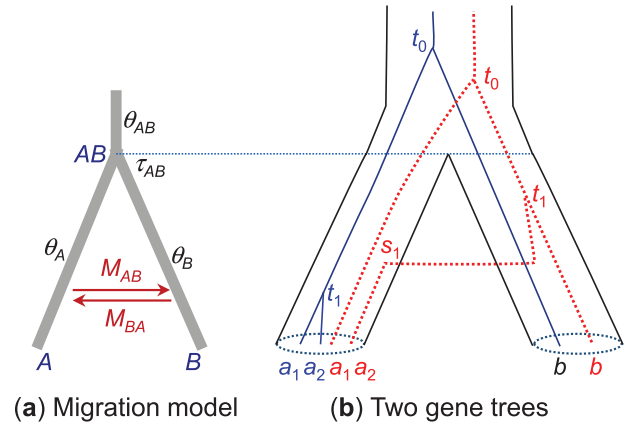


FIGURE 2. a) An MSC-M model for 2 species or populations (A, B) showing the parameters. The 2 populations diverged time $\tau_{AB} \equiv \tau$ ago and have since been exchanging migrants at the rate of $M_{AB} = m_{AB}N_B$ migrants per generation from A to B (under the real-world view with time running forward) and at the rate $M_{BA} = m_{BA}N_A$ from B to A . b) Two gene trees, each for 2 A sequences and 1 B sequence (a_1, a_2, b). In the blue tree (solid lines), a_1 and a_2 coalesce first (at time t_1), in population A , resulting in the gene tree $G_1 = ((a_1, a_2), b)$. This is G_{1a} of Figure 1. In the red tree (dotted lines), a_2 “migrates” (i.e., is traced back) into B at time s_1 and coalesces with b in B at time t_1 , resulting in the gene tree $G_2 = ((a_2, b), a_1)$. This is G_{2a} of Figure 1.

be modelled using the migration (MSC-M) model, with 6 parameters, $\Theta = (\tau_{AB}, \theta_A, \theta_B, \theta_{AB}, M_{AB}, \text{ and } M_{BA})$ (Fig. 2a). Similarly to the case of no gene flow, Jackson et al. (2017) defined $P_1 = \mathbb{P}(G_1|\Theta)$ to be the probability of gene tree G_1 , and rescaled it to define the gdi as

$$gdi_j = \frac{P_1 - \min(P_1)}{\max(P_1) - \min(P_1)}. \quad (3)$$

The limits $\min(P_1) = 1/3$ and $\max(P_1) = 1$ are used in the CalculateGdi function in PHRAPL (Jackson et al. 2017), which estimates P_1 by using Hudson’s (2002) ms program to simulate gene trees. When there is gene flow the minimum value achievable by P_1 depends on the migration events allowed in the model and on how the parameters in the model change, and it is possible for P_1 to be $< 1/3$, in which case the definition of Equation (3) with $\min(P_1) = 1/3$ leads to negative gdi values. We describe 2 such scenarios below.

One approach to dealing with negative gdi values is to set them to 0. Another is to modify the definition of Jackson et al. (2017). We note that with no gene flow, Equation (2) is simply the probability for gene tree G_{1a} (Fig. 1), or the probability that the first coalescence is between a_1 and a_2 and that this coalescence occurs before population split when we trace the genealogy of the 3 sequences backwards in time. In other words, we may define gdi as

$$gdi_K = \mathbb{P}(G_{1a}|\Theta) \quad (4)$$

under both the MSC model with no gene flow and the MSC-M model with gene flow. There is then no need for

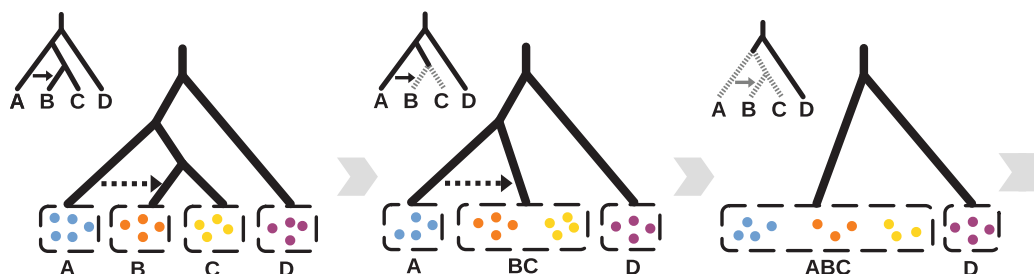
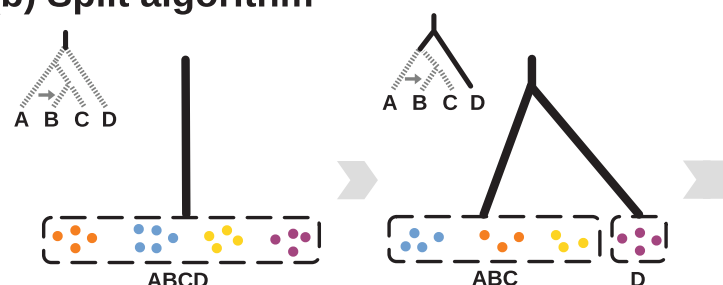
(a) Merge algorithm**(b) Split algorithm**

FIGURE 3. a) Hierarchical merge and b) hierarchical split algorithms applied to the same guide tree for 4 populations. The merge algorithm groups sister populations into 1 species only if $gdi < 0.2$, while the split algorithm splits 1 species into 2 only if $gdi > 0.7$. Because of the different cutoffs used, the merge algorithm may suggest more species than the split algorithm.

rescaling as $\mathbb{P}(G_{1a})$ ranges from 0 to 1. This definition is expected to work if A and B are non-sister lineages, and if there is gene flow from other populations into either A or B (see below for examples). The definition may also work if gene flow occurs in pulses as in the MSC-I model (Flouri et al. 2020), although this is not pursued here. With no gene flow, the 2 definitions (gdi_j and gdi_k) are equivalent but they may differ if there is gene flow.

An ambiguity arises when gdi can be calculated with reference both to A (using aab data or sequences a_1, a_2, b) and to B (using abb data or sequences a, b_1, b_2), leading to 2 indexes,

$$\begin{aligned} gdi_A &= 1 - e^{-2\tau_{AB}/\theta_A} = 1 - e^{-T_{AB}/2N_A}, \\ gdi_B &= 1 - e^{-2\tau_{AB}/\theta_B} = 1 - e^{-T_{AB}/2N_B} \end{aligned} \quad (5)$$

in the case of no gene flow (cf Equation (2)). If $N_A \ll N_B$, population A may appear to be a distinct species from B judged by gdi_A , but B may not appear to be a distinct species from A according to gdi_B (Leaché et al. 2019). Another major factor for such conflicting gdi indexes is the asymmetry in gene flow ($M_{AB} \neq M_{BA}$; see below). In our implementation, a merge is accepted if either gdi_A or gdi_B is less than the cut-off (0.2), whereas in the split algorithm, the split is accepted if both indexes are >0.5 and at least one of them is >0.7 .

The Hierarchical Merge and Split Algorithms

The hierarchical merge and split algorithms are illustrated in Figure 3. Both require the specification of

a guide tree, possibly with gene flow. This may be based on the prior knowledge of the taxonomist or previous phylogenetic analyses of genetic or morphological data. We assume that specimens or samples are already assigned to populations, which represent potentially distinct species. Our algorithms may group different populations into 1 species but never separate 1 population into multiple species. Prior knowledge may be used to specify migration events involving extant or extinct species/populations on the guide tree.

In the merge algorithm, we progressively group populations into the same species, starting from the tips of the tree and moving toward the root. A merge is accepted if either of the 2 gdi indexes (Equation (5)) is <0.2 . The algorithm stops when no population pair can be merged (Fig. 3a).

In the hierarchical split algorithm, we start from the model of 1 species and progressively split each species into distinct species, starting from the root and moving toward the tips of the guide tree (Fig. 3b). The split is accepted if both gdi indexes (Equation (5)) are >0.5 and at least one is >0.7 . The algorithm stops when no species can be split (Fig. 3b).

The merge and split algorithms are implemented under both the MSC model with no gene flow (Rannala and Yang 2003; Flouri et al. 2018) and the MSC-M model with migration (Flouri et al. 2023). Under the MSC-M model, we retain the migration event in the merge algorithm when at least 1 of the 2 merged populations is involved in migration with a third species. For example,

in the guide tree of [Figure 3a](#), there is migration from A to B . When B and C are merged into 1 species/population (BC), we retain the migration event (now from population A to population BC). When A and BC are later merged, the now intra-population migration event is removed.

In analysis of any dataset both the merge and split algorithms should be applied. We note that the merge and split algorithms may produce different results, mainly because of the different cutoffs (0.2 versus 0.7) and the large interval of indecision (with $0.2 < gdi < 0.7$), not because of the different algorithms (merge versus split). Under the model of no gene flow and if the gdi for each internal node is smaller than that for its mother node, the merge and split algorithms using the same cut-off will arrive at the same model of delimitation and phylogeny. Thus, one could run the merge (or split) algorithm alone, but twice, using the 2 cutoffs (0.2 and 0.7), and obtain the same 2 sets of results as our merge and split algorithms. It is also possible to use the cutoff 0.7 for merge and 0.2 for split, in which case the merge algorithm may delimit fewer species than split (an example is shown in [Supplementary Table S2](#)). In our current approach, the merge algorithm may infer more species than the split algorithm and the approach has a computational advantage as it may involve fewer BPP runs. Of course, this reasoning serves as a rough guide only, as it may not apply when there is gene flow in the model and when a mother node has a smaller gdi than a daughter node.

Computation of gdi Given Model Parameters

Given the parameters in the MSC or MSC-M models, we use different methods to calculate gdi , depending on the presence and types of migration events involving the focal populations A and B . We consider 3 cases: (a) no gene flow into A or B , (b) gene flow between A and B but not from any other populations, and (c) gene flow from other populations into at least one of A and B .

(a) In case of no gene flow into A or B , gdi_j and gdi_K are equivalent and [Equation \(4\)](#) simplifies to [Equation \(2\)](#), which is used in the calculation. Note that gene flow from populations A and B into a third population does not affect our calculation of gdi for A and B or our assessment of the species status of A and B .

(b) If there is migration between A and B but no gene flow from any other population into A or B , we use the Markov chain theory developed in the structured coalescent to calculate $gdi_K = \mathbb{P}(G_{1a})$ analytically.

Given 2 populations (A and B) with gene flow, the process of coalescent and migration when one traces the genealogical history of the sample (of sequences a_1, a_2, b) backwards in time can be described by a Markov chain, in which the states are specified by the number of sequences remaining in the sample and the population IDs (A and B) and sequence IDs (a_1, a_2, b) ([Supplementary Table S1](#)) ([Hobolth et al. 2011](#); [Zhu and Yang 2012](#);

[Jiao and Yang 2021](#)). The initial state is $A_{a_1}A_{a_2}B_b$, with 3 sequences a_1, a_2, b in populations A , A , and B , respectively. This is also written “AAB”. State $A_{a_1}A_{a_2}B_b$, abbreviated “AB_b,” means that sequences a_1 and a_2 have already coalesced so that 2 sequences remain in the sample, with the ancestor of a_1 and a_2 in A while b is in B . Finally state $A|B$ is an artificial absorbing state, in which all 3 sequences have coalesced with the sole ancestral sequence in either A or B . There are 21 states in the Markov chain, with the transition rate (generator) matrix $Q = \{q_{ij}\}$ given in [Supplementary Table S1](#) ([Leaché et al. 2019](#)).

The transition probability matrix over time t is then $P(t) = \{p_{ij}(t)\} = e^{Qt}$, where $p_{ij}(t)$ is the probability that the Markov chain is in state j at time t (in the past) given that it is in state i at time 0 (the present time). Suppose Q has the spectral decomposition

$$q_{ij} = \sum_{k=1}^{21} u_{ik} v_{kj} \lambda_k, \quad (6)$$

where $0 = \lambda_1 > \lambda_2 \geq \dots \geq \lambda_{21}$ are the eigenvalues of Q , and columns in $U = \{u_{ij}\}$ are the corresponding right eigenvectors, with $V = \{v_{ij}\} = U^{-1}$. Then

$$p_{ij}(t) = \sum_{k=1}^{21} u_{ik} v_{kj} e^{\lambda_k t}. \quad (7)$$

Gene tree G_{1a} arises if sequences a_1 and a_2 coalesce first and before τ (as in the blue gene tree of [Fig. 2b](#)), and the coalescence can occur in either populations A or B . The coalescent time t has the density

$$f(t) = [p_{AAB,AAA}(t) + p_{AAB,AAB}(t)] \frac{2}{\theta_A} + [p_{AAB,BBA}(t) + p_{AAB,BBB}(t)] \frac{2}{\theta_B}, \quad t < \tau. \quad (8)$$

The 2 terms in the sum correspond to the coalescence occurring in A and B , respectively. For example, the first term is the probability that both a_1 and a_2 are in A right before time t (corresponding to states AAA or AAB), $p_{AAB,AAA}(t) + p_{AAB,AAB}(t)$, times the coalescent rate $2/\theta_A$. Similarly the second term is the probability density that a_1 and a_2 coalesce at time t in B , given by the probability that a_1 and a_2 are in B right before time t times the coalescent rate $2/\theta_B$.

By averaging over the distribution of t , we have

$$gdi_K = \mathbb{P}(G_{1a}) = \int_0^\tau f(t) dt. \quad (9)$$

To calculate the integral in [Equation \(9\)](#), note that from [Equation \(7\)](#),

$$\int_0^\tau p_{ij}(t) dt = u_{i1} v_{1j} \tau + \sum_{k=2}^{21} u_{ik} v_{kj} \frac{e^{\lambda_k \tau} - 1}{\lambda_k}. \quad (10)$$

Furthermore, the probability for gene tree G_{1b} (Fig. 1) is

$$\mathbb{P}(G_{1b}) = p_{AAB,s_3}(\tau) \times \frac{1}{3}, \quad (11)$$

where $s_3 = \{AAA, AAB, ABA, ABB, BAA, BAB, BBA, BBB\}$ is the set of states with 3 sequences. For G_{1b} to occur, there must be no coalescence in the time interval $(0, \tau)$ and all 3 sequences must reach time τ , and then the 3 sequences coalesce in random order. Thus

$$\mathbb{P}(G_1) = \mathbb{P}(G_{1a}) + \mathbb{P}(G_{1b}), \quad (12)$$

from which gdi_j (Equation (3)) can be calculated.

(c) When populations A or B are recipients of gene flow from other populations, analytical calculation of the gdi becomes complicated. It is simpler to simulate a large number (10^6 or 10^7 , say) of gene trees under the migration model. Note that other populations on the guide tree than the focal populations A and B may contribute migrants into A or B . Parameters in the MSC-M model (τ_s , θ_s , and M) involving all those populations are estimated by *BPP* from the data. Gene trees for only 3 sequences (a_1, a_2, b) are then simulated, with no samples taken from other populations (see [Supplementary Fig. S1](#) for an example control file for such simulation). The gdi_K is simply the proportion for gene tree G_{1a} , that is, G_1 with $t_1 < \tau_{AB}$, among simulated gene trees (Fig. 1):

$$gdi_K = \mathbb{P}(G_{1a}) \approx \frac{\# \text{ of gene tree } G_{1a}}{R}, \quad (13)$$

where R is the number of replicate loci or gene trees.

Note that in cases (a) and (b), one could also use simulation to calculate gdi , but the analytical calculation is more accurate and computationally more efficient.

Uncertainty in gdi

The above describes the calculation of gdi given the parameters in the model (either with or without gene flow). In real data analysis, parameters are estimated from the sequence data and involve uncertainties due to the finite nature of data. A simple approach is to use the posterior means of parameters to calculate gdi . A more proper approach is to treat gdi as a function of the parameters and generate its posterior distribution and to use the posterior mean of gdi in the algorithm. The 2 approaches should be very similar if the dataset is informative and the parameters are well estimated.

Let $\{\Theta^{(i)}\}$ be the parameter values sampled from the MCMC (with the definition of Θ depending on the model). Then for each i , calculate $gdi^{(i)} = gdi(\Theta^{(i)})$ using 1 of the 3 approaches discussed in the last subsection. These $gdi^{(i)}$ values constitute a sample from the posterior distribution and can be used to calculate the posterior mean, and can also be sorted to generate

the 95% equal-tail credible interval (CI). The 95% highest probability density (HPD) CI can be calculated by sliding the 95% equal-tail CI to the left and to the right until the induced interval cannot be made shorter, relying on the fact that the HPD interval is the shortest (Chen and Shao 1999; see Fig. 7.14 in Yang 2014). We implemented a simple algorithm under the assumption that the HPD CI consists of 1 interval rather than several non-overlapping subintervals. Note that for the MSC-M model involving gene flow from other populations into A or B (case c), this procedure involves simulating many gene trees for each set of parameters $\Theta^{(i)}$. Thus, we may “thin” the MCMC sample to use only 1000 sets of parameter values.

Implementation of *HHSD*

Our pipeline creates control files and *Imap* files to drive the analyses using *BPP* (an *Imap* file maps individual samples to species/populations under the specified species-delimitation hypothesis). It then examines the *BPP* output to calculate gdi to attempt to merge populations or split species. If any merge (or split) occurs the species tree is modified and new *BPP* control and *Imap* files are generated for the next iteration of the hierarchical algorithm. The pipeline is itself driven by a control file. Many of the control variables are the same as used in *BPP*, and the same syntax is used between the 2 programs as much as possible.

Here, we illustrate our pipeline through an analysis of a multilocus sequence dataset simulated under the isolation-by-distance model of Figure 4a (Leaché et al. 2019). The *HHSD* control file is shown in Figure 5. There are 5 populations, with A, B, C, D representing populations of a species with a wide geographic distribution, while X is a new species that split off from population A . There is extensive gene flow between any 2 neighbouring populations of species $ABCD$, with migration rate $M = Nm = 2$ immigrants per generation, whereas there is no gene flow involving X (Fig. 4a). The data consisted of $L = 2000$ loci, with $S = 4$ sequences per species per locus, and 500 sites in the sequence.

The guide tree of Figure 4b, which is the starting delimitation for the merge algorithm, was generated using species tree estimation under the MSC model with no gene flow (i.e., the A01 analysis of Yang 2015). A manual run of the procedure is recorded in [Supplementary Table S2](#) (using the cutoff $gdi < 0.2$). The *HHSD* pipeline provides feedbacks about the current species delimitation and the decisions made during each iteration of the algorithm (Fig. 4c and [Supplementary Fig. S2](#)). In the first iteration, attempt was made to merge populations A and B , and C and D . As $gdi < 0.2$ for each pair, both merges were accepted. In the second iteration, a merge between AB and CD was attempted, and again this was accepted. In the third iteration, a merge between the pair $ABCD$ and X was attempted. As $gdi > 0.2$, the merge

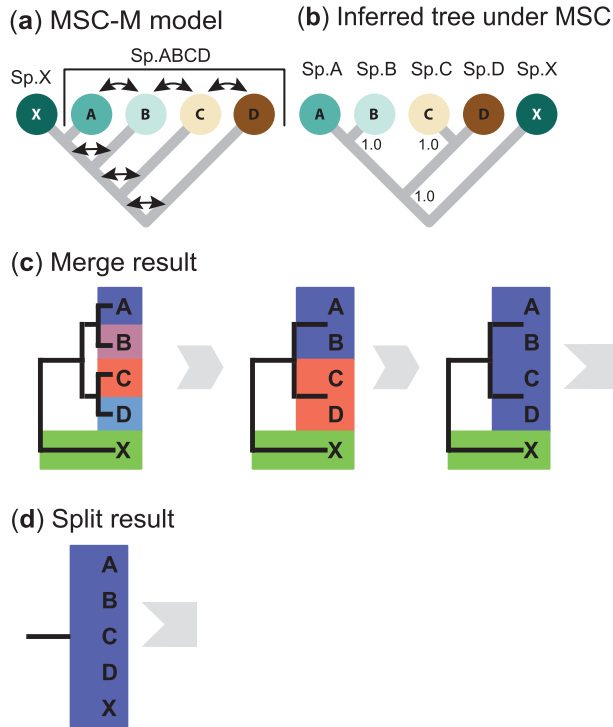


FIGURE 4. a) An isolation-by-distance model in which populations A, B, C, and D represent geographical populations of the same species, while population X is a distinct species that split from and remains in complete isolation with population A. The model is used to simulate multilocus sequence data. The parameters used are $\tau_{XABCD} = 0.04$, $\tau_{XABC} = 0.03$, $\tau_{XAB} = 0.02$, and $\tau_{XA} = 0.01$ for divergence times, and $\theta = 0.01$ for all populations, with $M = Nm = 2$ between any 2 adjacent populations of the species ABCD. Redrawn after Leaché et al. (2019, Fig. 5). b) Incorrect species delimitation and phylogeny produced in Bayesian model selection using BPP under the MSC model assuming no gene flow, with every node receiving 100% posterior support. c) Output from the hhsd pipeline applying the merge algorithm under the MSC model to the simulated data (see Fig. 5 for the control file). The species tree of panel b) is used as the guide tree (initial delimitation). A merge is accepted if either gdi_A or gdi_B is < 0.2 . The algorithm recognizes 2 species: X and ABCD. d) Output from the split algorithm. A split is accepted if both gdi_A and gdi_B are > 0.5 and at least one of them is > 0.7 . The algorithm infers 1 species (XABCD). The same data were also analyzed under the MSC-M model; see Supplementary Table S3 and text.

was rejected. The final delimitation had 2 species, ABCD and X.

Behavior of the gdi Under Models of Gene Flow

The pattern of gene flow under the MSC-M model may be very complex in terms of the number of gene-flow events, the lineages involved, and the directions and rates of gene flow. Gene flow is also known to exert profound impacts on the genealogical history of sequences sampled from modern species (Leaché et al. 2014; Long and Kubatko 2018; Jiao et al. 2020; Jiao and Yang 2021). Here, we characterize the behavior of the gdi under a few simple scenarios of gene flow,

```
# output
output_directory = res_sim_merge

# input files
Imapfile = starting_imap.txt
seqfile = sequences.txt

# guide tree
guide_tree = (X,((A,B),(C,D)));

# hierarchical algorithm settings
mode = merge
gdi_threshold = <=0.2, <=1.0

# BPP MCMC settings
threads = 12
burnin = 50000
nsample = 200000
```

FIGURE 5. Control file (simulated_merge_analysis.txt) for hhsd merge analysis of the data simulated under the model of Figure 4a. The control variables are as follows: output_directory specifies the output directory in which result files will be written; seqfile is the sequence alignment file in PHYLIP format; Imapfile specifies the assignment of individuals to populations; guide_tree is a Newick representation of the guide tree; and mode specifies the algorithm (merge or split). GDI_threshold specifies the gdi value below which 2 populations are merged into 1 species. threads specifies the number of CPU threads used to run BPP, while burnin, sampfreq, and nsample specify the MCMC settings for running BPP. Run hhsd using the command

```
hhsd --cfile simulated_merge_analysis.txt
```

and leave it to the future to explore more complex models.

Case (a) Symmetrical migration model for 2 populations.— The symmetrical migration model for 2 populations, with $N_A = N_B = N$ and $M_{AB} = M_{BA} = M$ (Fig. 2a), has been used by Jackson et al. (2017) and Leaché et al. (2019) to calculate gdi_j (Equation (3)). Under this model, both gdi_j and gdi_K are functions of 2 parameters: $2\tau/\theta = T/(2N)$ and M . In Figure 6 we plot gdi_j and gdi_K for a range of values for those 2 parameters. Overall large population split time and low migration rate correspond to high gdi values and the species status of the 2 populations.

The 2 definitions (gdi_j and gdi_K) are very similar in the whole parameter space except for the Northeast corner where both the migration rate and population split time are large. In such a scenario, the 2 populations should be considered 1 species according to gdi_j (Fig. 6a), while the species status is ambiguous according to gdi_K (Fig. 6b). The 2 indexes represent different biological interpretations of the same population divergence history, akin to 2 species concepts. We leave it to the future to evaluate which of them better matches the experience and expectation of taxonomists.

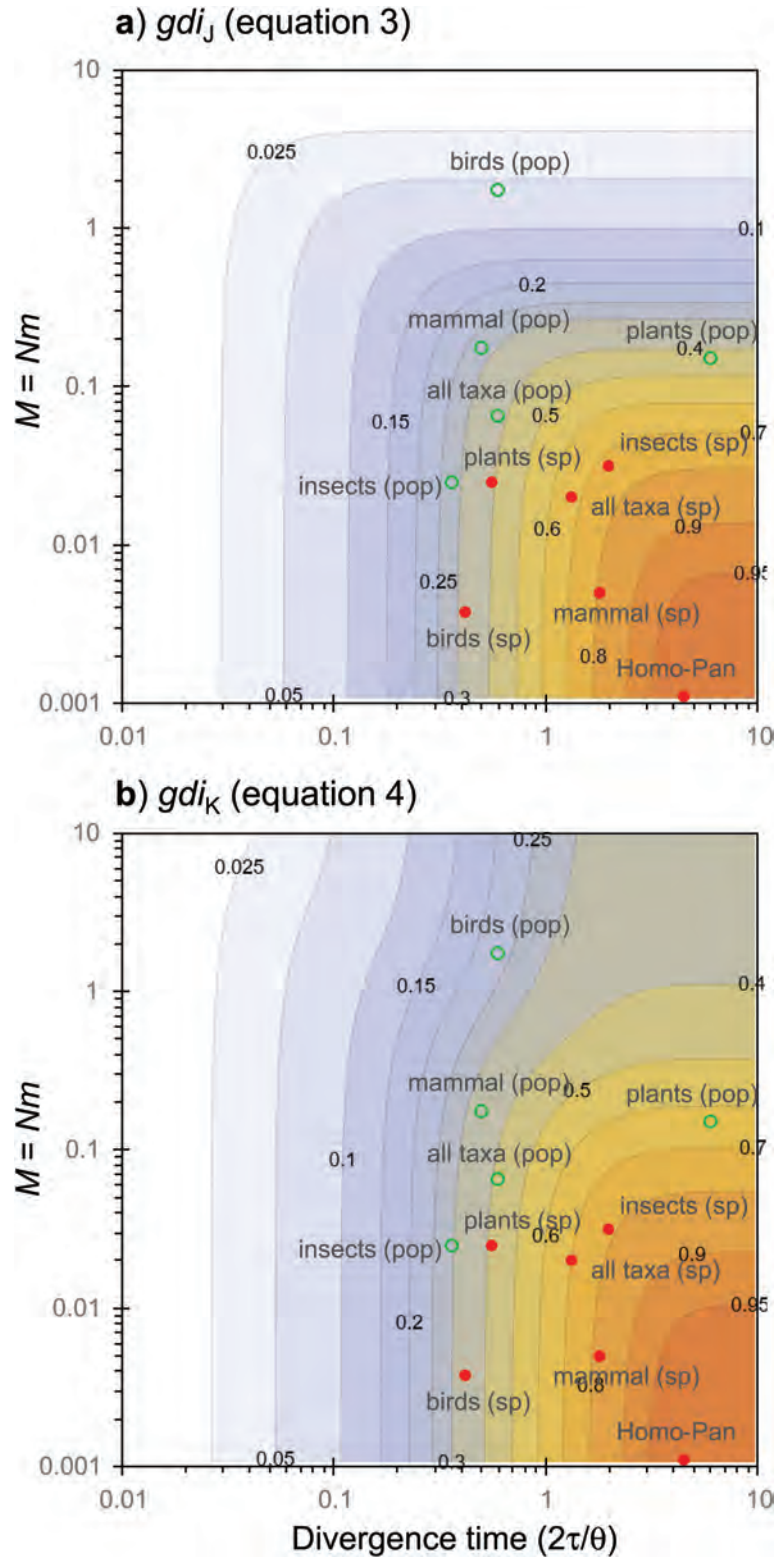


FIGURE 6. [Case a] a) gdi_j and b) gdi_K plotted against the population split time in coalescent units ($2\tau/\theta = T/2N$) and the population migration rate ($M = Nm$) under the symmetrical migration model for 2 populations, with $\theta_A = \theta_B = \theta$ and $M_{AB} = M_{BA} = M$ (Fig. 2a). The cut-offs at 0.2 and 0.7 are indicated by red contour lines. The green circles (between populations) and red dots (between species) represent median values of empirical estimates from major taxonomic groups (mammals, birds, insects, and plants) from the meta-analysis of Jackson et al. (2017, Fig. 6), based on data compiled by Pinho and Hey (2010, Supplementary Table S1). Panel a) is a transformation of $\mathbb{P}(G_1)$ of Leaché et al. (2019, Fig. 3) using Equation (2). Under this symmetrical MSC-M model, there is no difference between gdi_A and gdi_B of Equation (5) and also gdi_j is always > 0 .

Case (b) Asymmetrical gene flow between 2 populations. — Next, we consider an MSC-M model of unidirectional gene flow for 2 populations, with $M_{BA} > 0$ and $M_{AB} = 0$. This is a special case of the general model of Figure 2a considered in the Theory section and is analytically tractable. To track the history of sequences a_1, a_2, b up to the split time τ , we use the generator matrix $Q^{(1)}$ of Jiao and Yang (2021):

	AAB	ABB	BAB	BBB	AB _b	A _{a1} B	A _{a2} B	BB _{b1}	B _{a1} B	B _{a2} B	B
AAB	$-2\omega - c_A$	ω	ω	0	c_A	0	0	0	0	0	0
ABB	0	$-\omega - c_B$	0	ω	0	c_B	0	0	0	0	0
BAB	0	0	$-\omega - c_B$	ω	0	0	c_B	0	0	0	0
BBB	0	0	0	$-3c_B$	0	0	0	c_B	c_B	c_B	0
AB _b	0	0	0	0	$-\omega$	0	0	ω	0	0	0
A _{a1} B	0	0	0	0	0	$-\omega$	0	0	ω	0	0
A _{a2} B	0	0	0	0	0	0	$-\omega$	0	0	ω	0
BB _{b1}	0	0	0	0	0	0	0	$-c_B$	0	0	c_B
B _{a1} B	0	0	0	0	0	0	0	0	$-c_B$	0	c_B
B _{a2} B	0	0	0	0	0	0	0	0	0	$-c_B$	c_B
B	0	0	0	0	0	0	0	0	0	0	0

where $\omega = 4M/\theta_A = m_{BA}/\mu$, $c_A = 2/\theta_A$, and $c_B = 2/\theta_B$.

Let $P(t) = \{p_{ij}(t)\} = e^{Qt}$. To derive $gdi_K = \mathbb{P}(G_{1a})$, let $t < \tau$ be the coalescent time for sequences a_1 and a_2 . As in Equation (8), this has density

$$f(t) = p_{AAB,AAB}(t) \cdot c_A + p_{AAB,BBB}(t) \cdot c_B, \quad t < \tau, \quad (14)$$

where the 2 terms represent coalescence in populations A and B, respectively. Then

$$\begin{aligned} \mathbb{P}(G_{1a}) &= \int_0^\tau f(t) dt \\ &= \frac{4e_1\theta_B^2M^2}{3(M\theta_B - \theta_A)(3\theta_A - \theta_B - 4M\theta_B)} \\ &\quad + \frac{4e_2\theta_A\theta_B^2M^2}{(\theta_A - M\theta_B)(\theta_A + 2M\theta_B)(\theta_A - 2M\theta_B - \theta_B)} \\ &\quad + \frac{3\theta_A + 2M(4M + 3)\theta_B}{3(1 + 4M)(\theta_A + 2M\theta_B)} - \frac{e_3}{1 + 4M} \\ &\quad - \frac{8e_3\theta_A\theta_BM^2}{(\theta_A - \theta_B - 2M\theta_B)(3\theta_A - \theta_B - 4M\theta_B)(1 + 4M)}, \end{aligned} \quad (15)$$

where $e_1 = \exp\{-6\tau/\theta_B\}$, $e_2 = \exp\{-4M\tau/\theta_A - 2\tau/\theta_B\}$ and $e_3 = \exp\{-2(1 + 4M)\tau/\theta_A\}$.

Let $s_3 = \{AAB, ABB, BAB, BBB\}$ be the set of states with 3 sequences. We have $\mathbb{P}(G_{1b}) = p_{AAB,s_3}(\tau) \cdot 1/3$, and

$$\begin{aligned} \mathbb{P}(G_1) &= \mathbb{P}(G_{1a}) + \mathbb{P}(G_{1b}) = \\ &\frac{4\theta_A\theta_Bc_3e_4(1 + 4M)M - \theta_A\theta_B(8M^2 - 3) - \theta_A\theta_Bc_3(8M^2 + 2)}{3(1 + 4M)(\theta_A + 2\theta_BM)(\theta_B + 2\theta_BM - \theta_A)} \\ &\quad + \frac{(2e_3 - 4Me_3 - 3)\theta_A^2 + 2\theta_B^2M(2M + 1)(4M + 3 - 2e_3)}{3(1 + 4M)(\theta_A + 2\theta_BM)(\theta_B + 2\theta_BM - \theta_A)}, \end{aligned} \quad (16)$$

where $e_4 = \exp\{4M\tau/\theta_A + 2\tau/\theta_A - 2\tau/\theta_B\}$.

Both gdi_I and gdi_K are functions of 3 parameters: $2\tau/\theta_A = T/(2N_A)$, M , and N_A/N_B . Figure 7b,c shows that gdi_I can be negative under this model. If population A has a much larger size than B, the 2 A sequences may not coalesce in A, and 1 of them may migrate into

B (with time running backwards) and coalesce with sequence b, resulting in gene trees $G_2 = ((a_2, b), a_1)$ or $G_3 = ((b, a_1), a_2)$. As a result, gene tree G_1 may be less probable than G_2 or G_3 , creating an anomaly: 2 sequences from A are on average more distant from each other than either is from a sequence from B (Jiao and Yang 2021). See also Figure 2a in Jiao and Yang (2021).

In Figure 8a,b, we plot gdi_I and gdi_K against M and $2\tau/\theta_A$, with $\theta_A/\theta_B = 5$ fixed (the precise value of θ_A does not matter). In Figure 8c,d, we plot gdi_I and gdi_K against M and θ_A/θ_B , with $\tau = 5\theta_B$ fixed (the precise value of θ_B does not matter). The 2 indexes behave in the same way except in the case of high migration rate and long divergence time, where gdi_I lumps the 2 populations into 1 species, whereas gdi_K is indecisive. This is the same pattern as under the symmetrical migration model of Figure 6.

We also considered the gdi with reference to population B, using sequences a, b_1, b_2 . We use the following generator matrix Q until the split time τ :

	ABB	BBB	A _a B	B _a B	BB _{b1}	BB _{b2}	B
ABB	$-\omega - c_B$	ω	c_B	0	0	0	0
BBB	0	$-3c_B$	0	c_B	c_B	c_B	0
A _a B	0	0	$-\omega$	ω	0	0	0
B _a B	0	0	0	$-c_B$	0	0	c_B
BB _{b1}	0	0	0	0	$-c_B$	0	c_B
BB _{b2}	0	0	0	0	0	$-c_B$	c_B
B	0	0	0	0	0	0	0

where $\omega = m_{BA}/\mu$ and $c_B = 2/\theta_B$.

Let $P(t) = \{p_{ij}(t)\} = e^{Qt}$. The coalescent time $t < \tau$ for sequences b_1, b_2 has density

$$f(t) = [p_{ABB,ABB}(t) + p_{ABB,BBB}(t)] \cdot c_B, \quad t < \tau, \quad (17)$$

so that

$$\begin{aligned} \mathbb{P}(G_{1a}) &= \int_0^\tau f(t) dt \\ &= \frac{3\theta_A^2 - 2\theta_B^2M^2 - \theta_A\theta_BM - 3e_1e_2\theta_A^2 + e_1\theta_BM(\theta_A + 2\theta_BM)}{3(\theta_A - M\theta_B)(\theta_A + 2M\theta_B)}, \end{aligned} \quad (18)$$

where $e_1 = \exp\{-6\tau/\theta_B\}$ and $e_2 = \exp\{-4M\tau/\theta_A + 4\tau/\theta_B\}$.

As $\mathbb{P}(G_{1b}) = [p_{ABB,ABB}(\tau) + p_{ABB,BBB}(\tau)] \cdot \frac{1}{3}$, we have

$$\mathbb{P}(G_1) = \mathbb{P}(G_{1a}) + \mathbb{P}(G_{1b}) = \frac{(3 - 2e_3)\theta_A + 2M\theta_B}{3(\theta_A + 2M\theta_B)}, \quad (19)$$

where $e_3 = \exp\{-4M\tau/\theta_A - 2\tau/\theta_B\}$.

Again both gdi_I and gdi_K are functions of 3 parameters: $2\tau/\theta_A = T/(2N_A)$, M , and N_A/N_B . In Figure 9a,b, we plot gdi_I and gdi_K for *abb* data (using sequences a, b_1, b_2) over the same parameter space as in Figure 8. For *abb* data, the differences

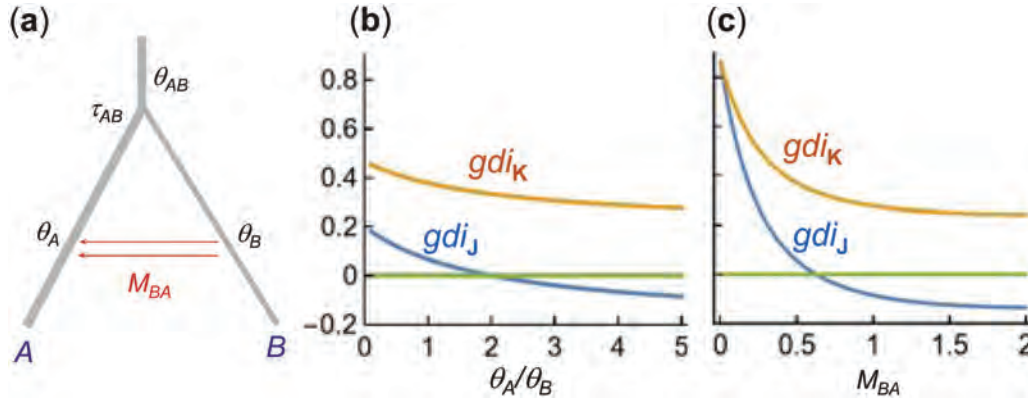


FIGURE 7. [Case b, *aab* data] a) An asymmetrical migration model for 2 populations (*A*, *B*) with migration from *B* to *A*. There are 5 parameters in the model, but gdi_J and gdi_K depend on only 3: $2\tau/\theta_A = T/(2N_A)$, $M = M_{BA}$, and $\theta_A/\theta_B = N_A/N_B$. b and c) gdi_J and gdi_K plotted against N_A/N_B or M_{BA} , with $\tau = 5\theta_B$ (the precise value of θ_B does not matter). In b), $M_{BA} = 1$ is fixed, while in c), $\theta_A/\theta_B = 5$ is fixed. When N_A/N_B in b) or M in c) is large, the probability for the gene tree $G_1 = ((a_1, a_2), b)$ may be $< \frac{1}{3}$, so that $gdi_J < 0$.

between gdi_J and gdi_K are small (cf: Fig. 9a,b). However, there are large differences between gdi_A and gdi_B of Equation (5), reflecting the dramatic influence of the relative population sizes on the perceived species status of the populations (cf: Figs. 8c and 9c and Figs. 8d and 9d). For very small N_A/N_B , it is possible for $gdi_A > 0.7$ and $gdi_B < 0.2$. When population *A* has a much smaller size than population *B*, population *A* may appear to be a distinct species from *B*, while population *B* appears to be of the same species as *A*.

Case (c) Gene flow from a ghost species.—Markov chain at time τ . In the model of Figure 10a, populations *A* and *B* have been in complete isolation since they diverged time $\tau_{AB} = \tau$ ago, but a more distant population *C* which diverged at time τ_{ABC} has been contributing migrants into population *A* at the rate of $M_{CA} = M$ migrants per generation. We sample sequences a_1 and a_2 from *A* and b from *B*, with no sample from *C*. The genealogical history of sequences a_1 and a_2 until time τ is described by a Markov chain with 4 states: *AA*, *AC*, *CC*, *A|C*, with the last being an absorbing state after the 2 sequences have coalesced. The generator matrix Q is

	<i>AA</i>	<i>AC</i>	<i>CC</i>	<i>A C</i>
<i>AA</i>	$-(2\omega + c_A)$	2ω	0	c_A
<i>AC</i>	0	$-\omega$	ω	0
<i>CC</i>	0	0	$-c_C$	c_C
<i>A C</i>	0	0	0	0

where $\omega \equiv \omega_{CA} = m_{CA}/\mu$, $c_A = 2/\theta_A$ and $c_C = 2/\theta_C$. The eigenvalues of Q are $\lambda_1 = 0$, $\lambda_2 = -c_C$, $\lambda_3 = -c_A - 2\omega$, and $\lambda_4 = -\omega$.

Let $P(t) = \{p_{ij}(t)\} = e^{Qt}$. Given the initial state *AA*, the transition probabilities into the 4 states over time τ are

$$\begin{aligned}
 p_{11} &= e^{-(c_A + 2\omega)\tau}, \\
 p_{12} &= \frac{2\omega}{c_A + \omega} [e^{-\omega\tau} - e^{-(c_A + 2\omega)\tau}], \\
 p_{13} &= \frac{2\omega^2 [(c_C - \omega)e^{-(c_A + 2\omega)\tau} - (c_A + \omega)e^{-c_C\tau} + (c_A - c_C + 2\omega)e^{-\omega\tau}]}{(c_A + \omega)(c_C - \omega)(c_A - c_C + 2\omega)}, \\
 p_{14} &= 1 - p_{11} - p_{12} - p_{13} \equiv \mathbb{P}(G_{1a}).
 \end{aligned}
 \tag{20}$$

Note that the transition probability $p_{14}(\tau)$ is also $gdi_K = \mathbb{P}(G_{1a})$ of Equation (4). The probability for gene tree G_1 is given by averaging over the 4 possible states of the Markov chain at time τ ,

$$\begin{aligned}
 \mathbb{P}(G_1) &= p_{11} \times \frac{1}{3} + p_{12} e^{-2\Delta\tau/\theta_{AB}} \times \frac{1}{3} \\
 &\quad + p_{13} (1 - \frac{2}{3} e^{-2\Delta\tau/\theta_C}) + p_{14},
 \end{aligned}
 \tag{21}$$

with $\Delta\tau = \tau_{ABC} - \tau_{AB}$, while $\mathbb{P}(G_2) = \mathbb{P}(G_3) = (1 - \mathbb{P}(G_1))/2$. The first term in Equation (21) corresponds to state *AA*, with both a_1 and a_2 remaining in *A* at time τ (with probability p_{11}). Then all 3 sequences enter population *AB* and coalesce in random order, so that gene tree G_1 occurs with probability $\frac{1}{3}$. The second term corresponds to state *AC* at time τ , which means that one of a_1 and a_2 is in *A* with the other in *C*. If the sequence in *A* does not coalesce with b in the ancestral population *AB*, then gene tree G_1 will occur with probability $\frac{1}{3}$. The third term corresponds to state *CC*, with both a_1 and a_2 in *C* at time τ (with probability p_{13}). Then gene tree G_1 arises if a_1 and a_2 coalesce in *C* or in *ABC*. The fourth term, p_{14} , corresponds to state *A|C*, in which a_1 and a_2 have coalesced (in either *A* or *C*) before reaching τ so that the gene tree is G_1 (also G_{1a}) (Fig. 1).

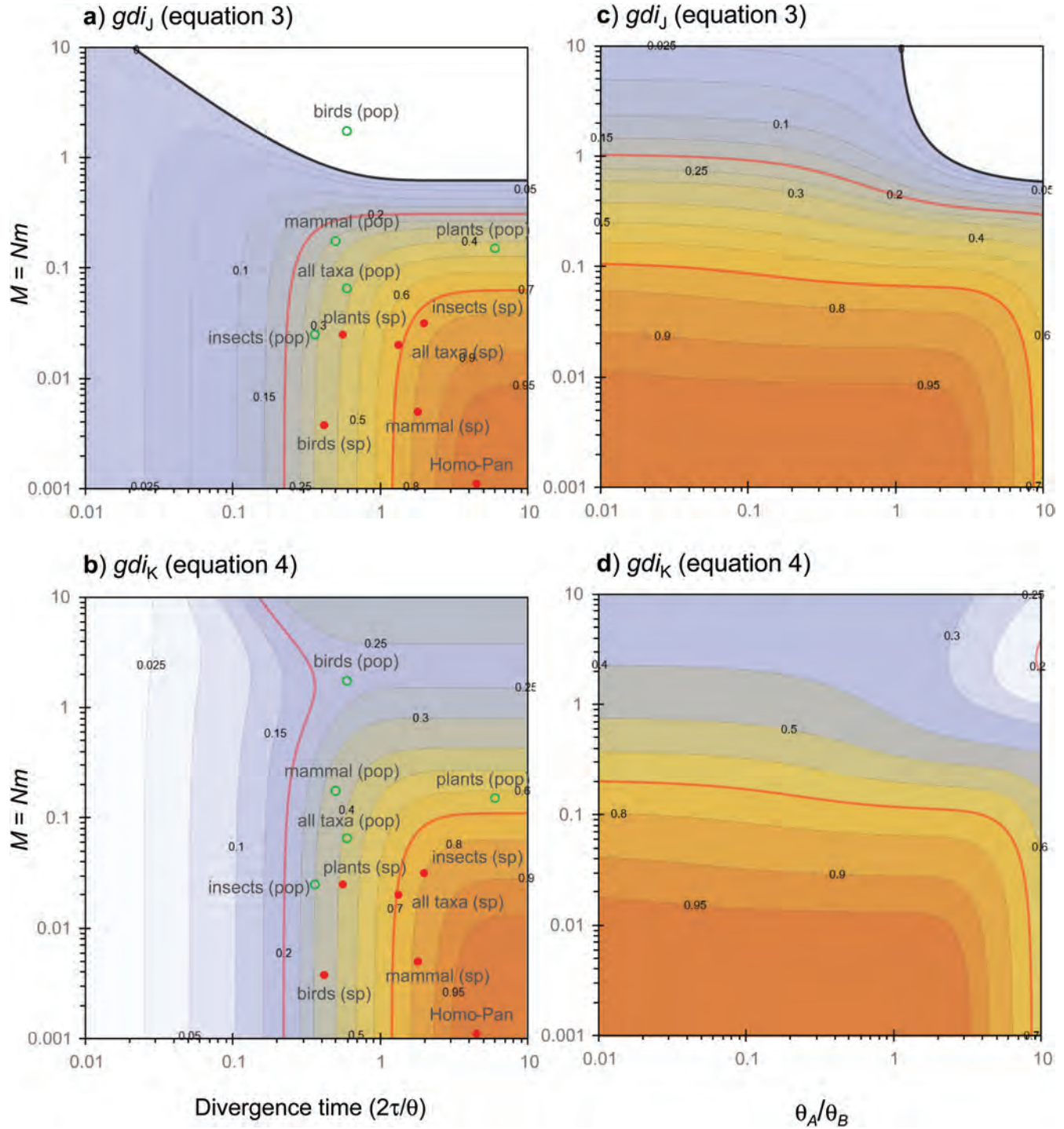


FIGURE 8. [Case b, *aab* data] a) gdi_j and b) gdi_K for sequences a_1, a_2, b under the unidirectional migration model of Figure 7a, plotted against $M = M_{BA}$ and $2\tau/\theta_A$, with $\theta_A/\theta_B = 5$ (the precise value of θ_A does not matter). c and d) Plots under the same model against M and θ_A/θ_B , with $\tau = 5\theta_B$. In a) and c), $gdi_j < 0$ in the white region outside the black contour line.

The MSC-M model of Figure 10a involves 8 parameters, $\Theta = (\tau_{ABC}, \tau_{AB}, \theta_A, \theta_B, \theta_C, \theta_{AB}, \theta_{ABC}, \text{ and } M_{CA})$, but the gene-tree probability $\mathbb{P}(G_1)$ is a function of 5: $2\tau/\theta_A = T_{AB}/(2N_A)$, $c_A/c_C = N_C/N_A$, M_{CA} , $\Delta\tau/\theta_{AB}$,

and $\Delta\tau/\theta_C$. The new index $gdi_K = \mathbb{P}(G_{1a})$ is a function of the first 3 parameters.

As in the unidirectional migration model of Figure 7a, a similar anomaly arises under the model of Figure 10a

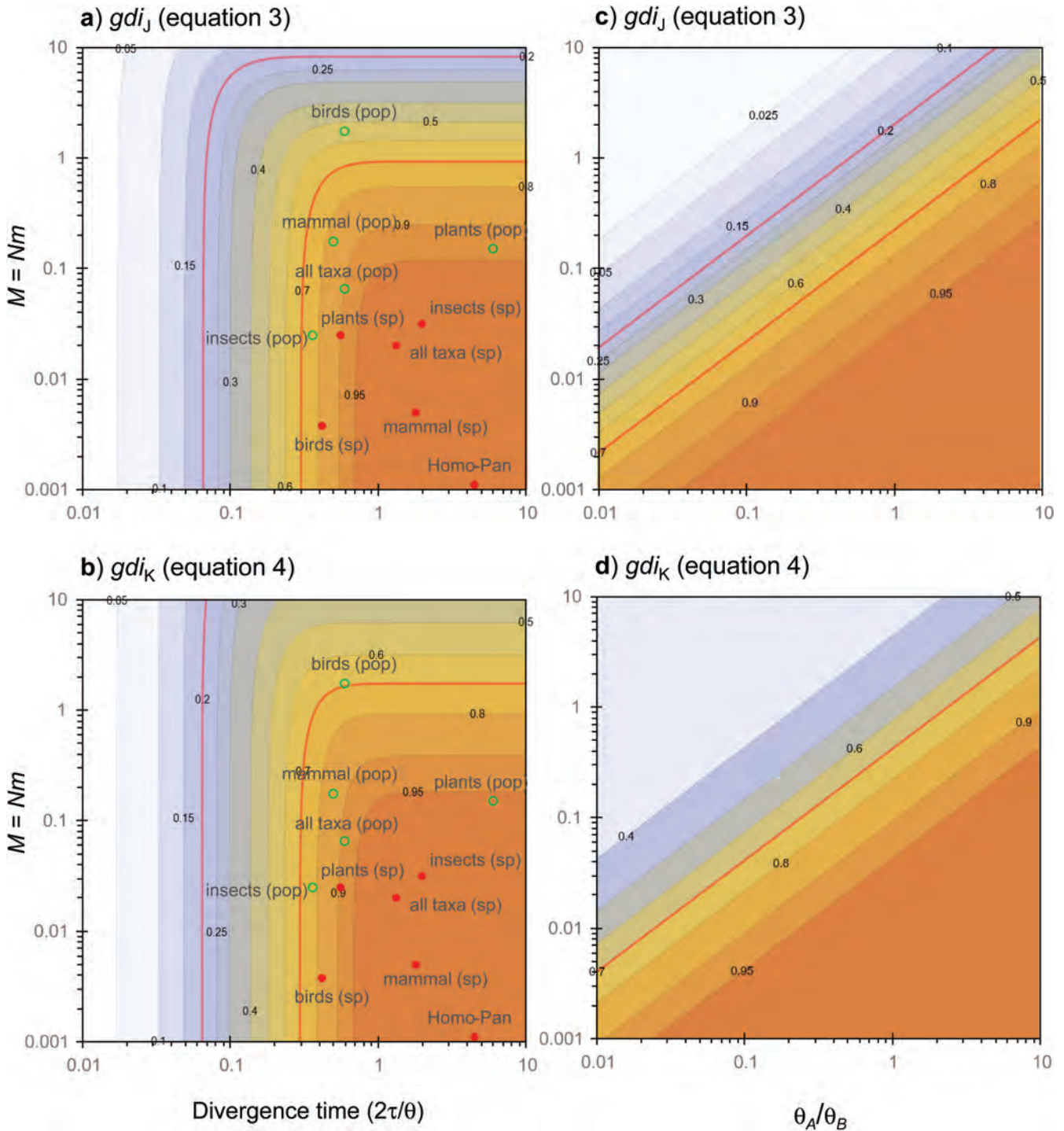


FIGURE 9. [Case b, for *abb* data] a) gdi_j and b) gdi_K for sequences a, b_1, b_2 under the unidirectional migration model of Figure 7a, plotted against $M = M_{BA}$ and $2\tau/\theta_A$, with $\theta_A/\theta_B = 5$. c and d) Plots under the same model against M and θ_A/θ_B , with $\tau = 5\theta_B$. The model and parameter space are the same as in Figure 8 for *aab* data, and here gdi_j is always positive.

with gene flow from a ghost species (Fig. 10b,c). For example, when the parameters are $\tau_{ABC} = 0.01$, $\tau_{AB} = 0.005$, $\theta_A = \theta_C = 0.05$, $\theta_{AB} = 0.001$, and $M_{CA} = 1$, we have $\mathbb{P}(G_1) = 0.2995 < \frac{1}{3}$ (Equation (21)), giving

$gdi_j = -0.0508$. This is confirmed by simulation [see Supplementary Fig. S1 for the BPP control file for simulating gene trees in this case; parameters such as $\theta_{ABC} = 0.01$ are needed to run the simulation program but do

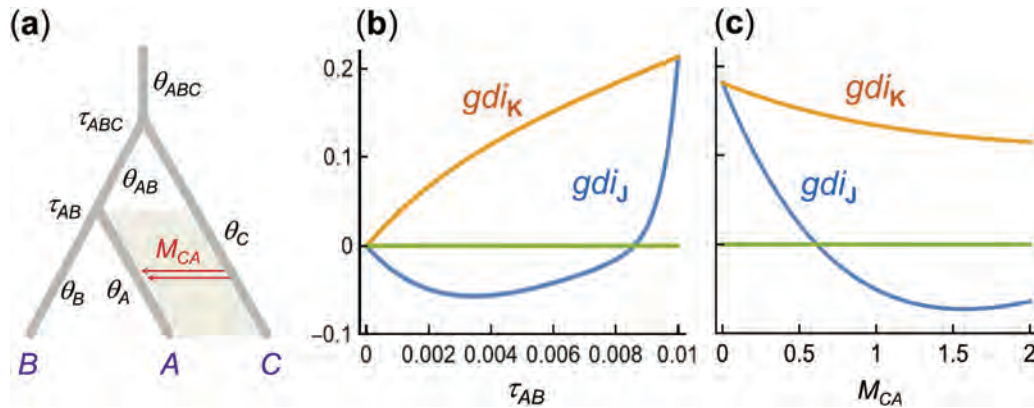


FIGURE 10. [Case c, *aab* data] a) An MSC-M model for 3 species (A, B, C) with migration from a ghost species C to A. In part of the parameter space, the probability for the gene tree $G_1 = ((a_1, a_2), b)$ is $< \frac{1}{3}$, with $gdi_j < 0$ (Equation (3)). b and c) gdi_j and gdi_K plotted against τ_{AB} or M_{CA} with $\tau_{ABC} = 0.01$, $\theta_A = \theta_C = 0.05$, and $\theta_{AB} = 0.001$. In b), $M_{CA} = 1$ is fixed, while in c), $\tau_{AB} = 0.005$ is fixed.

not affect $\mathbb{P}(G_1)$. As either of a_1 and a_2 may migrate into C (backwards in time), reducing the chance for a_1 and a_2 to coalesce in population A, gene tree G_1 may be less probable than G_2 or G_3 , with $\mathbb{P}(G_1) < \mathbb{P}(G_2) = \mathbb{P}(G_3)$.

In Figure 11a,b we plot gdi_j and gdi_K against M_{CA} and $2\tau/\theta$, with other parameters fixed at the values of Figure 10. For those parameter values, gdi_j and gdi_K are very similar, although $gdi_j < 0$ in part of the parameter space.

If we use instead *abb* data (with sequences a, b_1, b_2), we have

$$\mathbb{P}(G_1) = 1 - \frac{2}{3} e^{-2\tau/\theta_B}, \quad \mathbb{P}(G_{1a}) = 1 - e^{-2\tau/\theta_B},$$

as in the case of no gene flow, and $gdi_j = gdi_K$.

There is thus a major asymmetry in the gdi index (Equation (5)) under this model: while gdi_A for *aab* data depends on 5 or 3 parameters (for gdi_j and gdi_K , respectively), gdi_B for *abb* data depends on another unrelated parameter ($2\tau/\theta_B$). All possible scenarios are thus possible concerning gdi_A versus gdi_B . For example, *aab* data may recognize A as a distinct species from B, while *abb* data may recognize B as of the same as A, or vice versa.

Case (d) Gene flow between non-sister lineages and paraphyletic species.—Finally, we considered the species tree and MSC-M model of Figure 4a, in which populations A, B, C, and D represent 1 paraphyletic species with excessive gene flow between them, while population X is a distinct species that split off from population A time τ_{XA} ago and has since been in complete isolation from population A or species ABCD. We conducted 2 analyses under the model. The first was an assessment of the gdi calculated for non-sister populations (such as A and B in Fig. 4a). The second was a re-analysis of the multilocus sequence data simulated under the model of Figure 4a,

to explore the idea of merging non-sister lineages under the MSC-M model in the hierarchical merge algorithm to delimit paraphyletic species.

First, we explored the behavior of the gdi for non-sister populations. We simulated gene trees to calculate gdi for population pairs X–A, A–B, B–C, and C–D at different migration rates, with $M = 0, 0.01, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5, 0.75, 1, 1.5$, and 2. Other parameters are given in Figure 4a. For each M and each population pair, we simulated gene trees for 3 sequences (in either the *aab* or *abb* configuration) to calculate gdi_j and gdi_K . For instance, for populations A and B and the *aab* configuration, we simulated 10^6 gene trees for 3 sequences (a_1, a_2, b) under the MSC-M model for 5 populations of Figure 4a and calculated the proportions of gene tree G_1 as well as G_{1a} , that is, $G_1 = ((a_1, a_2), b)$ with the node age $t_{aa} < \tau_{XAB}$.

The results are shown in Figure 12. If there is little gene flow, with $M = Nm \leq 0.05$, all 5 populations (X, A, B, C, D) are considered distinct species using both indexes gdi_j and gdi_K , and using both *aab* or *abb* data. However, at moderate levels of gene flow, the results depend on the index and the data configuration.

Concerning the species status of X and A, the 2 indexes gdi_j and gdi_K are very similar, but there are substantial differences depending on whether one calculates gdi using *xxa* or *xaa* data. When one uses *xxa*, $gdi > 0.7$ (Fig. 12a,c, X–A pair), and population X is judged to be a distinct species from A. However, with *xaa* data, $gdi < 0.7$ when $M > 0.1$ (Fig. 12b,d, X–A pair), and population A may not be considered a distinct species from X. The difference may be due to the fact that because of gene flow from population B, population A has a much larger effective population size than X.

Concerning the species status of populations A, B, C, and D, the data configuration (*aab* vs. *abb*) made little difference, but the 2 indexes gdi_j and gdi_K behaved

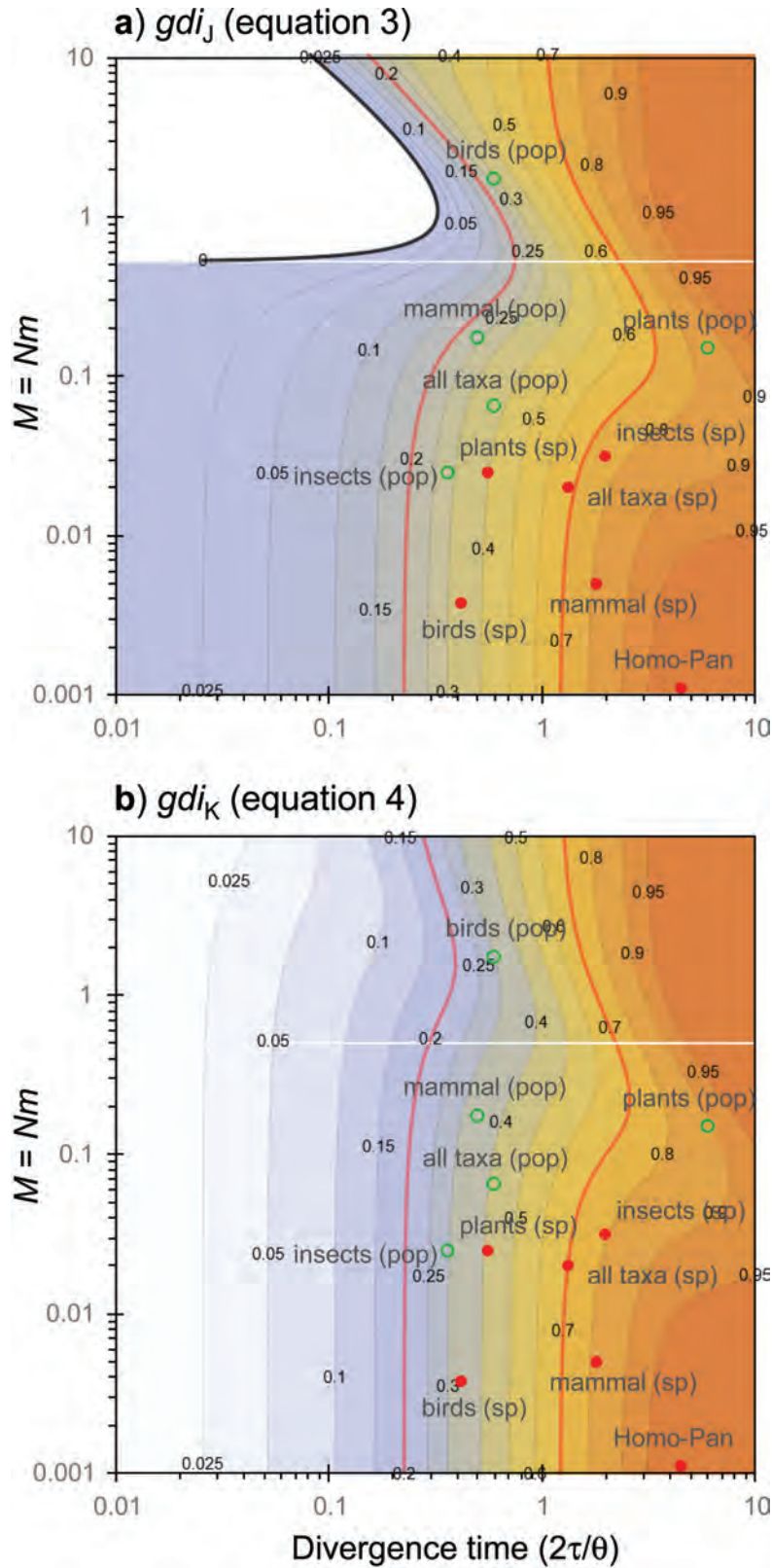


FIGURE 11. [Case c, *aab* data] a) gdi_J and b) gdi_K for sequences a_1, a_2, b under the MSC-M model of Figure 10a with gene flow from a ghost species, plotted against $M = M_{CA}$ and $2\tau/\theta$, with $\theta_A = \theta_C = \theta$, and $\Delta\tau = 0.1\theta_C = 5\theta_{AB}$. In a), $gdi_J < 0$ in the white region outside the black contour line. We used the parameter values of Figure 10 in the calculation, but note that gdi_J depends on only 5 parameters and gdi_K depends on 3.

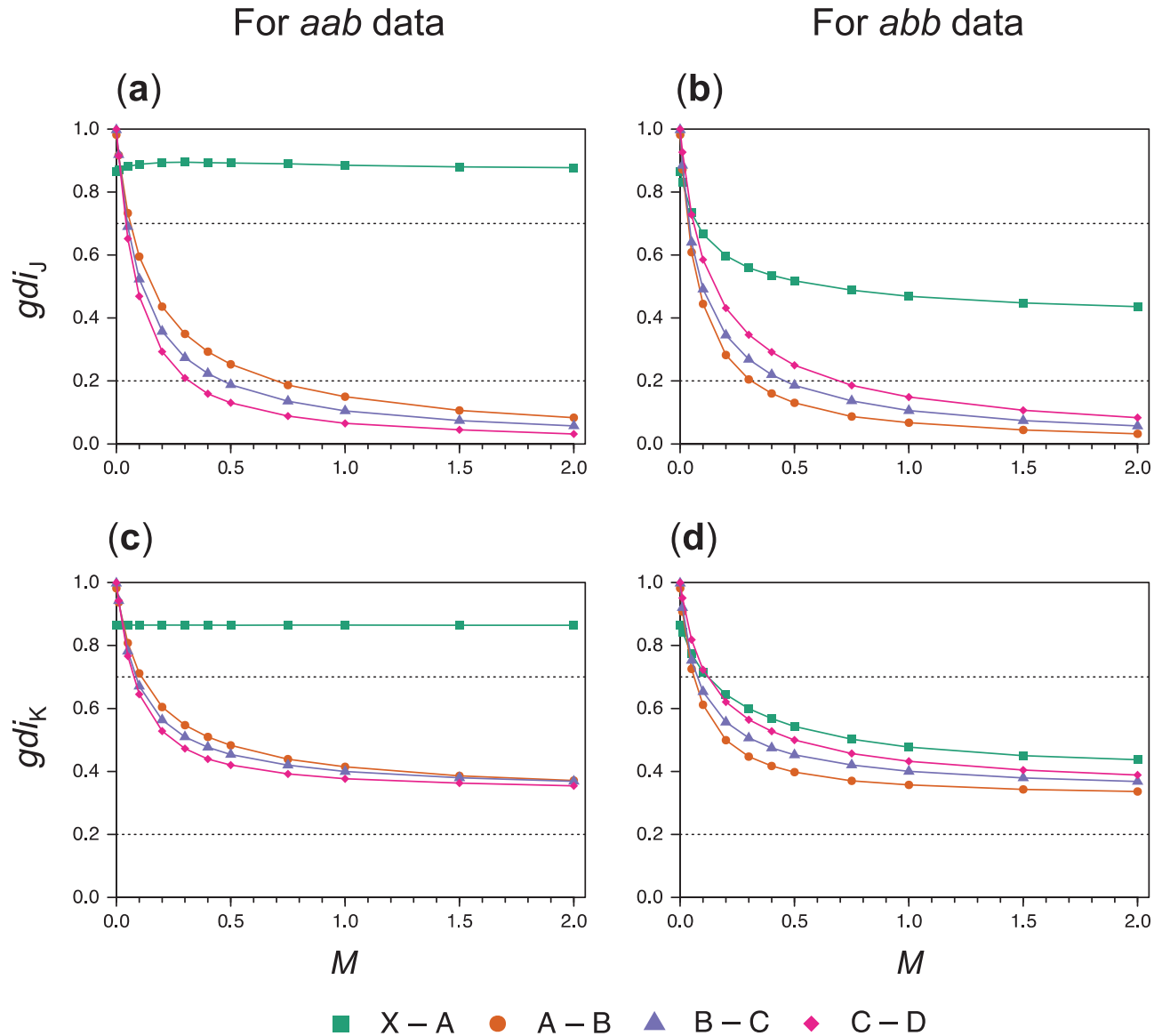


FIGURE 12. gdi_j and gdi_K for population pairs under the isolation-by-distance model of Figure 4a, plotted against the migration rate ($M = Nm$), estimated by simulating 10^6 gene trees for 3 sequences. Parameters are fixed at the values in Figure 4a: $\tau_{XABCD} = 0.04$, $\tau_{XABC} = 0.03$, $\tau_{XAB} = 0.02$, and $\tau_{XA} = 0.01$, with $\theta = 0.01$ for all populations. Three sequences, in either the *aab* or *abb* configuration, are sampled per locus per population pair; in the case of populations *A* and *B*, they are either a_1, a_2, b , in which case the gene tree G_1 has the topology $((a_1, a_2), b)$; or a, b_1, b_2 , in which case G_1 is $(a, (b_1, b_2))$.

differently. When $M > 0.5$, gdi_j assigned populations *A*, *B*, *C*, and *D* to the same species ($gdi_j < 0.2$, Fig. 12a,b), while gdi_K is indecisive ($0.2 < gdi_K < 0.7$, Fig. 12c,d). This appeared to be the same pattern as in the symmetrical migration model of case (a) (Fig. 6).

Second, we analyzed the XABCD dataset simulated under the MSC-M model of Figure 4a. Earlier these data were analyzed under the MSC model with no gene flow, using the guide tree of Figure 4b, which had a different topology from the true species tree of Figure 4a. With no gene flow in the model, gdi_j and gdi_K are equivalent,

and both inferred either 1 species (XABCD) at the cutoff of $gdi = 0.7$ or 2 species (*X* and ABCD) at the cutoff of $gdi = 0.2$.

Here, we re-analyzed the same data under the MSC-M model, allowing the merge of non-sister populations as a strategy for delimiting paraphyletic species. We ignored the problem of inferring the MSC-M model with gene flow from genomic data (see Flouri et al. 2023 for discussions), and used the true MSC-M model of Figure 4a as the guide tree (or starting delimitation). In each iteration, we allow the merging of multiple pairs

of sister lineages. If no sister pair can be merged, we consider non-sister pairs and allow the merge of only 1 non-sister pair (corresponding to the smallest *gdi*). After each merge, migration events between the merged populations are removed. Two cutoffs, 0.2 and 0.7, are used in the algorithm. This procedure is not yet automated in the HHSD pipeline, and instead we implemented it manually (Supplementary Table S3). *gdi_j* supported 2 species (*X* and *ABCD*) at the cutoff *gdi* < 0.2 or 1 species at the cutoff *gdi* < 0.7. In contrast, *gdi_K* identified 5 species at the cutoff *gdi* < 0.2 or 1 species (*XABCD*) at the cutoff *gdi* < 0.7. The results agreed well with the theoretical calculations of Figure 12.

RESULTS FROM EMPIRICAL DATASETS

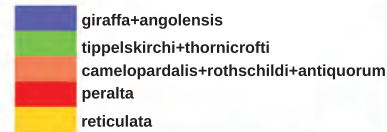
We analyzed 3 empirical datasets using the HHSD pipeline. In each case, the specific taxonomic group and associated delimitation problem will be introduced along with existing results.

Species Delimitation of Giraffes (Genus *Giraffa*)

The taxonomic position and classification of giraffes (genus *Giraffa*) have been controversial for many years (Mitchell 2009). Previous studies using morphological characters and molecular data produced inconsistent results, delimiting from 1 to 6 species in the *Giraffa* genus. Currently, 9 geographical populations are recognized as subspecies: *camelopardalis*, *angolensis*, *antiquorum*, *giraffa*, *peralta*, *reticulata*, *rothschildi*, *thornicrofti*, and *tippelskirchi*. Most recently, Petzold and Hassanin (2020) compiled a multilocus dataset of 21 introns (average sequence length 808 bp), sampled from 66 individuals from the 9 subspecies, and conducted a number of population genetic and phylogenetic analyses. The authors suggested a delimitation with 3 species, although they noted that Bayesian model selection by BPP supported as many as 5 species.

We re-analyzed these data using our pipeline, using the 5-species phylogeny (Fig. 13b) as the guide tree, which was inferred using BPP by Petzold and Hassanin (2020). Based on phylogenetic analysis of mitochondrial haplotypes and identified hybrids (Fennessy et al. 2016; Petzold and Hassanin 2020), bidirectional migration was specified between *reticulata* and the *tippelskirchi*+*thornicrofti* lineage, and between *reticulata* and the *camelopardalis*+*rothschildi*+*antiquorum* lineage. Migration rates were assigned the gamma prior $G(0.1, 10)$ with a mean of $0.1/10 = 0.01$ migrant individuals per generation. Merge and split analyses were conducted with the animal-specific *gdi* thresholds of 0.3 and 0.7, as recommended by Jackson et al. (2017) (see Supplementary Fig. S3 for the control file). Each iteration of the algorithms took ~2h using 8 threads on a server with Intel Xeon Gold 6154 CPU, with a total runtime of approximately 8 h.

(a) Distribution



(b) Guide tree



(c) Merge result



(d) Split result

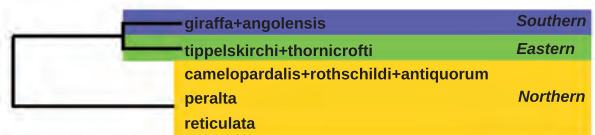


FIGURE 13. a) Geographical distributions of 5 putative species within *Giraffa*. The bright region on the map (modified from <https://giraffeconservation.org/giraffe-species/>) shows historical (ca. 1700) giraffe ranges. b) The guide tree for 5 populations of giraffes, with gray arrows indicating bidirectional migration events (Petzold and Hassanin 2020, Fig. 1). c) The merge algorithm supports 5 species, while d) the split algorithm supports 3.

The merge algorithm suggested 5 species, while the split algorithm suggested 3 (Fig. 13c,d). Both methods recognized the Eastern (*tippelskirchi* and *thornicrofti*) and Southern (*giraffa* and *angolensis*) populations in the guide tree as distinct species. The split algorithm lumped the 3 Northern populations into 1 species, while the merge algorithm recognized them as 3 distinct species.

TABLE 1 Estimates (posterior means and 95% HPD CIs) of migration rates (M) between the 5 putative giraffe species in the guide tree of Figure 13b.

Donor	Recipient	M (95% HPD CI)
TipTho	reticulata	0.002 (0.000, 0.015)
reticulata	TipTho	0.002 (0.000, 0.009)
reticulata	CamRotAnt	0.027 (0.000, 0.129)
CamRotAnt	reticulata	0.123 (0.000, 0.328)

Estimates of migration rates during the merge algorithm supported the hypothesized patterns of gene flow between reticulated giraffes and the neighbouring populations (Table 1). The highest migration rate was between the Northern populations from *cam.+rot.+ant.* to *reticulata*.

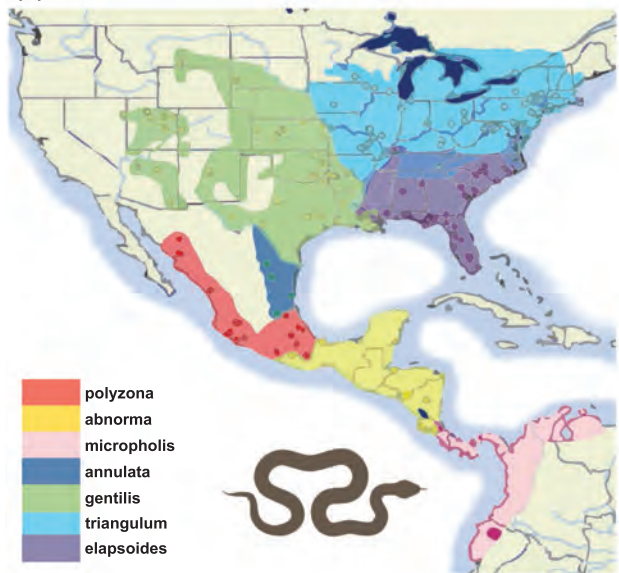
Species Delimitation in Milksnakes (*Lampropeltis triangulum*)

The American milksnake *Lampropeltis triangulum* is a New World snake with one of the widest known geographic distributions within the squamates. Seven subspecies are known: *abnorma*, *polyzona*, *micropholis*, *triangulum*, *gentilis*, *annulata*, and *elapsoides* (Fig. 14a). Ruane et al. (2014) analyzed 11 nuclear loci (average length 537 bp) for 164 individuals from the 7 subspecies using BPP model comparison and found evidence for 7 distinct species. Chambers and Hillis (2020) re-analyzed these data and suggested that several species hypothesized by Ruane et al. (2014) may represent arbitrary slices of continuous geographic clines. They instead suggested 2 delimitation hypotheses, with 3 and 1 species, respectively, as shown in Figure 14c, d.

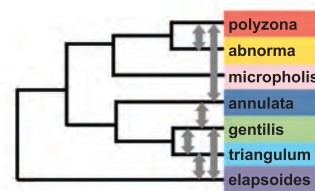
We re-analyzed the data of Ruane et al. (2014) using our pipeline, using the guide tree for 7 populations of Chambers and Hillis (2020) (Fig. 14b). As the original analysis Ruane et al. (2014) found ongoing gene flow between geographically adjacent populations, we added bidirectional migration events in the guide tree (Fig. 14b). Merge and split algorithms were run using *gdi* thresholds of 0.3 and 0.7 (see Supplementary Fig. S4 for the control file). Each iteration of the algorithm took ~ 2.5 h using 8 threads on a server, with a total runtime of ~ 12.5 h.

The merge algorithm suggested 3 species, grouping the subspecies *abnorma*, *polyzona*, and *micropholis* into 1 species, and *triangulum*, *gentilis*, and *annulata* into another species (Fig. 14c). This is the same delimitation as the 3-species hypothesis of Chambers and Hillis (2020). The split analysis supported only 1 species (Fig. 14d). Migration rates between the adjacent subspecies/populations during the merge analysis suggested ongoing genetic exchange between some of the subspecies pairs, in particular, between *L. annulata* and *L. gentilis*, and between *L. abnorma* and *L. polyzona* (Table 2).

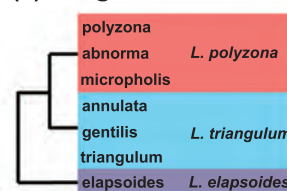
(a) Distribution



(b) Guide tree



(c) Merge result



(d) Split result



(e) Alternative East-West splits

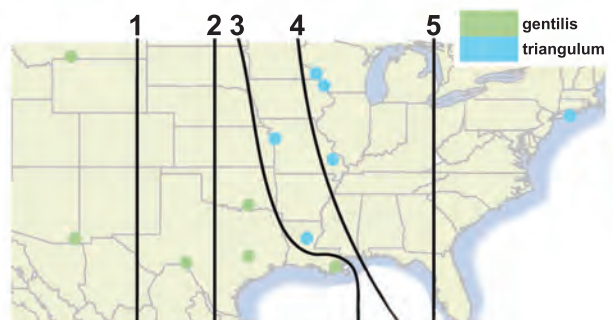


FIGURE 14. a) Geographic distribution of 7 milksnake subspecies (map based on and modified from Ruane et al. 2014, Fig. 1d). b) The guide tree with bidirectional migration events indicated by gray arrows. c and d) Inferred delimitation hypotheses by the merge and split algorithms. e) Alternative delimitation hypotheses tested by Chambers and Hillis (2020), each of which splits the *gentilis* and *triangulum* samples at an arbitrary West-East divide line. The HNSD merge algorithm grouped the 2 populations in each hypothesis into a single species.

TABLE 2 Estimates of migration rates (M) between 7 milksnake populations during the merge algorithm (Figure 14).

It.	Donor	Recipient	M (95% HPD CI)
1	elapsoides	gentilis	0.003 (0.000, 0.019)
	gentilis	elapsoides	0.010 (0.000, 0.055)
	elapsoides	triangulum	0.009 (0.000, 0.052)
	triangulum	elapsoides	0.055 (0.000, 0.152)
	annulata	polyzona	0.002 (0.000, 0.012)
	polyzona	annulata	0.003 (0.000, 0.016)
	annulata	gentilis	0.162 (0.000, 0.331)
	gentilis	annulata	0.053 (0.000, 0.220)
	polyzona	abnorma	0.044 (0.000, 0.189)
	abnorma	polyzona	0.127 (0.000, 0.293)
	gentilis	triangulum	0.011 (0.000, 0.070)
	triangulum	gentilis	0.050 (0.000, 0.267)
2	elapsoides	GenTri	0.008 (0.000, 0.049)
	GenTri	elapsoides	0.067 (0.000, 0.142)
	annulata	PolAbn	0.002 (0.000, 0.010)
	PolAbn	annulata	0.003 (0.000, 0.020)
	annulata	GenTri	0.081 (0.000, 0.276)
3	GenTri	annulata	0.073 (0.000, 0.181)
	elapsoides	AnnGenTri	0.016 (0.000, 0.085)
	AnnGenTri	elapsoides	0.102 (0.028, 0.184)
	MicPolAbn	AnnGenTri	0.006 (0.000, 0.034)
	AnnGenTri	MicPolAbn	0.080 (0.028, 0.135)

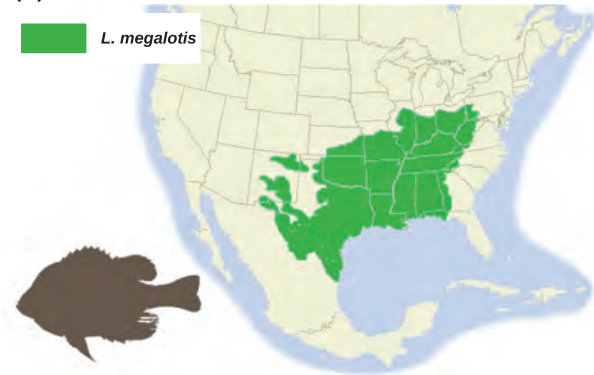
Chambers and Hillis (2020) also applied an arbitrary West-East divide to split the *gentilis* and *triangulum* populations into 2 species, generating 5 arbitrary delimitation hypotheses (each with 2 species) (Fig. 14e). They found that all 5 delimitation hypotheses were supported by Bayesian model selection using BPP, even though they are arbitrary. We used our pipeline to re-analyze the data, using the merge algorithm with the same settings as above. The data consisted of only the 38 individuals from *gentilis*, *triangulum*, and *annulata* populations. The same guide tree for the 3 populations was used, but each hypothesis was represented by constructing an Imap file to map the individual samples to the 3 populations (see Supplementary Figs. S5 and S6 for the control file and command-line scripts). Bidirectional migration between *gentilis* and *triangulum* was allowed in the guide tree. Each iteration of the algorithm took ~ 1.5 h on a server using 8 threads, with a total runtime of ~ 15 h.

Under each of the 5 delimitation hypotheses, the HSD merge algorithm grouped the 2 subspecies *gentilis* and *triangulum* into a single species.

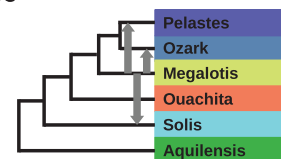
Introgression and Species Delimitation in the Longear Sunfish (*Lepomis megalotis*)

The longear sunfish (*Lepomis megalotis*) is a freshwater fish in the sunfish family, Centrarchidae, of the order Perciformes. It is native to eastern North America from the Great Lakes down to northeastern Mexico (Fig. 15a). Six subspecies are recognized: *aquilensis*, *solis*, *ouachita*, *megalotis*, *ozark*, and *pelastes*. Due to the widespread geographic distribution and frequent hybridization, species delimitation in the longear sunfish

(a) Distribution



(b) Guide tree



(c) Merge and split result

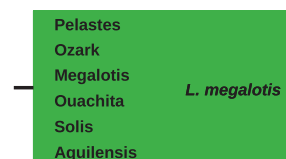


FIGURE 15. a) Geographic distribution of longear sunfish (*Lepomis megalotis*) (map based on <http://www.roughfish.com/content/longear-sunfish>). b) The guide tree, with 3 migration events (from *L. megalotis* to *L. pelastes*, *L. solis*, and *L. ozark*) indicated by gray arrows. c) Both merge and split algorithms support a single species.

poses considerable challenges. Kim et al. (2022) analyzed a dataset of 163 ddRAD loci (average sequence length 89 bp) sampled from 50 individuals from the 6 subspecies. After inferring a species/population phylogeny using IQ-TREE, they analyzed the data under the MSC model with no gene flow using BPP to calculate *gdi* scores to delimit species in the group. They found that none of the population pairs had high *gdi* values to support distinct species status. Kim et al. (2022) also found evidence for multiple instances of historical or ongoing gene flow.

We re-analyzed the data of Kim et al. (2022), using the MSC-M model to calculate *gdi*, accommodating migration between the subspecies. Based on the hybridization patterns observed by Kim et al. (2022), migration from *megalotis* to *pelastes*, *solis*, and *ozark* was specified in the guide tree (Fig. 15b). Migration rates were assigned the gamma prior $G(0.1, 10)$ with a mean of 0.01. Merge and split algorithms were run using *gdi* thresholds of 0.3 and 0.7 (control file in Supplementary Fig. S7). Each iteration of the algorithm took ~ 20 h using 16 threads, with a total runtime of ~ 120 h.

TABLE 3 Estimates of migration rates between 5 sunfish populations during the merge algorithm (Figure 15).

It.	Donor	Recipient	M (95% HPD CI)
1	megalotis	solis	0.605 (0.412, 0.808)
	megalotis	pelastes	0.537 (0.370, 0.709)
	megalotis	ozark	0.322 (0.103, 0.596)
2	megalotis	solis	0.692 (0.462, 0.945)
	megalotis	PelOzk	0.693 (0.397, 0.989)
3	PelOzkMeg	Solis	0.579 (0.387, 0.785)
4	PelOzkMegOua	Solis	0.407 (0.279, 0.541)

Both merge and split analyses supported a single species. This is congruent with the delimitation of Kim et al. (2022), in which gdi was calculated under the MSC model without gene flow. Estimates of the migration rates between the subspecies during the merge algorithm (Table 3) were consistently large, supporting the classification of those populations as a single species.

DISCUSSION

Heuristic Species Delimitation with Gene Flow and Paraphyletic and Polytypic Species

In this paper, we have developed a python pipeline to automate hierarchical merge and split algorithms for heuristic species delimitation. The merge algorithm was described and applied by Leaché et al. (2019), and here we have made the procedure automatic. We have also implemented the hierarchical split algorithm. Our tests using both simulated and empirical datasets suggest that the heuristic algorithms based on gdi may be less prone to over-splitting, which has been discussed extensively as a problem with the approach of Bayesian model selection implemented in BPP (Yang and Rannala 2010).

Heuristic species delimitation discussed here may be considered refinements of earlier heuristics including genetic-distance cutoffs (such as the “10× rule” in DNA barcoding, Hebert et al. 2004) and reciprocal monophyly of gene trees (Baum and Shaw 1995). For example, under the complete-isolation model (MSC with no gene flow), gdi (Equation (2)) is a simple function of $\tau/(\theta/2) = T/(2N)$, which contrasts within-species polymorphism with between-species divergence, just as does the “10x rule” — note that $2N$ is the average divergence time (in generations) between 2 sequences sampled from within the same species (of size N) while T is the species split time (in generations). Similarly gene tree $G_1 = ((a_1, a_2), b)$ is one of within-species monophyly given the 3 sequences at the locus (a_1, a_2, b) . Earlier criteria make use of simple summaries of the genetic data, whereas the methods discussed here are based on population parameters. Distinguishing data summaries from population parameters and adopting a statistical

inference framework makes it easy to address properly concerns such as gene-tree reconstruction errors due to lack of phylogenetic information, stochastic fluctuations of the coalescent process across the genome, etc. Note that reliable estimation of the species tree and population parameters is possible from analysis of genomic data even if every locus contains very weak phylogenetic information (Xu and Yang 2016). Indeed simulation studies suggest that genomic data provide rich information concerning population histories, and the MSC framework is powerful to produce precise and accurate estimation of population parameters (e.g., Huang et al. 2020; Thawornwattana et al. 2022; Ji et al. 2023). As gdi is defined as a function of parameters, by definition gdi will be well estimated from genomic data as well.

Our pipeline requires the user to supply a guide tree. This may be inferred using BPP under the MSC model with no gene flow (Yang and Rannala 2014; Rannala and Yang 2017). Other programs implementing the MSC may be used as well, such as *BEAST (Douglas et al. 2022) and IMA (Hey et al. 2018). Phylogenetic programs such as IQ-TREE (Minh et al. 2020) and RAxML (Stamatakis et al. 2012) may also be used to infer the maximum likelihood tree using concatenated genomic data or mitochondrial genomic sequences.

We note that the hierarchical merge and split algorithms implicitly assume a monophyletic species definition and thus do not work when a species is paraphyletic. Paraphyletic species, or species comprising of multiple populations that are not monophyletic, appear to be common (Crisp and Chandler 1996). Note that one may insist on higher taxa being always monophyletic while allowing for paraphyletic species (Crisp and Chandler 1996). The model tree of Figure 4a represents such a scenario, in which species ABCD is paraphyletic. The issue here concerns the non-monophyly of the populations of the same species, and is different from the monophyly of a gene tree, which is problematic if used as a criterion for species delimitation (Knowles and Carstens 2007). Non-monophyly of gene trees is a natural consequence of the coalescent process under the MSC model and can arise even if the populations of each species are monophyletic.

If all populations are completely isolated with no gene flow, the concept of a paraphyletic species does not appear to be sensible. For example, if the population phylogeny is the model of Figure 4a but without gene flow, that is, $((((X, A), B), C), D)$, it does not appear sensible to designate population X as a distinct species while lumping populations A, B, C , and D into 1 species, given that populations B, C , and D split from A earlier than X did. However, with gene flow between populations, the population divergence history may render the species to be paraphyletic (as in the model of Figure 4a with gene flow). In this study, we have explored 2 approaches to delimiting paraphyletic species or to accommodating gene flow during heuristic species delimitation.

The first is to use a guide tree for all populations (including those that make up the paraphyletic species) assuming no gene flow. This is used in Leaché et al. (2019, Fig. 3b) and in this paper, where the guide tree is constructed under the MSC model ignoring gene flow and then used to calculate the *gdi* (Fig. 4b,c). The resulting guide tree may reflect gene flow as well as population divergence (Fig. 4b,c) and may differ from the population phylogeny. For the simulated dataset of Figure 4, this led to delimitations of either 1 species at the cutoff of 0.7 or 2 species (ABCD and X) at the *gdi* = 0.2 cutoff (see also Supplementary Table S2). The results appeared sensible even though the guide tree used did not have the correct topology.

The second approach is to use the MSC-M model accommodating gene flow in the guide tree (e.g., the MSC-M model of Fig. 4a), but allow the merge of non-sister lineages involved in gene flow in the merge algorithm (e.g., A and B; Fig. 4a). When 2 non-sister populations are merged, one may use the idea of *displayed species trees* (Degnan 2018) to generate the new species tree or model. For example, if populations B and D are merged because of high migration rate M_{BD} , we may merge D into B so that the species tree becomes $((X,A),(B,D)),C$, whereas if M_{DB} is high, we may merge B into D to give the species tree $((X,A),C),(B,D))$. This approach is not yet implemented in *HHSD*, but we applied it manually to the simulated data of Figure 4a in Supplementary Table S3, and the results appeared sensible.

Even within the framework of Bayesian model selection, multiple approaches may be possible when there is gene flow between populations. Given populations A and B, 3 models may be considered: (i) H_1 : 1 single species, (ii) H_2 : 2 species with no gene flow, and (iii) H_{2m} : 2 species with gene flow (with either $M_{AB} > 0$ or $M_{BA} > 0$ or both). Leaché et al. (2019) compared H_1 and H_2 to decide whether there is 1 or 2 species, and noted that if a population split is followed by gene flow so that H_{2m} is the true model, then H_2 is less wrong than H_1 and will win over H_1 , potentially leading to over-splitting. Alternatively one may insist on species status only if there is no significant evidence for gene flow, that is, only if H_2 wins over both H_1 and H_{2m} . This may arguably be a more faithful implementation of the biological species concept (Dobzhansky 1937; Mayr 1942; Coyne and Orr 2004) than the comparison between H_1 and H_2 (Yang and Rannala 2010). However, this approach may lead to over-lumping since some “good” species are known to exchange migrants.

Challenges and Utility of Heuristic Species Delimitation

The greatest challenge to heuristic species delimitation, when applied to determine the species status of allopatric geographical populations, may be the arbitrary nature of species concept (e.g., de Queiroz 2007; Mallet et al. 2023; Maddison and Whitton 2023). Even if a full characterization of the history of the populations

is available, in terms of the order and timings of population splits, population sizes, and the directions, timings and strengths of gene flow between populations, a universally accepted view on species status may not exist. Darwin considered the difference between a species and a variety (subspecies, race, or population) to be one of degree, while Bateson (1909) considered species to have a “strict and concrete meaning in contradistinction to the term Variety” and suggested hybrid sterility as a test of species status. The biological species concept (Dobzhansky 1937; Mayr 1942; Coyne and Orr 2004) emphasizes reproductive isolation as the major criterion for species status. Thus, heuristic species delimitation discussed here is more in keeping with Darwin’s view that species are continuous, with fuzzy boundaries between species and “varieties” (subspecies, races, or populations). Allopatric populations that do not overlap in their geographical distributions, with no or little gene flow between them, may be classified as distinct species, or subspecies of a polytypic species, and some arbitrariness appears unavoidable.

The large interval of uncertainty for *gdi*: $0.2 < gdi < 0.7$ (Jackson et al. 2017) should be considered a consequence of the arbitrariness of the heuristic delimitation. This is also the main cause for different species delimitations in analysis of the same data using the same guide tree by the merge and split algorithms, as in our analyses of the giraffe and milksnake datasets (Figs. 13c,d and 14c,d). The cutoffs of Jackson et al. (2017) were based on estimates of population parameters in 178 empirical studies compiled by Pinho and Hey (2010, Supplementary Table S1). The datasets analyzed in those studies were small, mostly with only a few loci for 2 populations, and the summaries were medians of estimates in major taxonomic groups. It may be profitable to redo the meta-analysis, using more recent genomic sequence data and improved analytical methods to generate empirical estimates of population parameters in well-studied systems where the species status of the populations is well established. Such an effort may be hoped to lead to refined criteria and cutoffs (with reduced interval of uncertainty).

In our hierarchical algorithms, it should be straightforward to use empirical criteria other than the *gdi*. It is also possible to apply a composite criterion; for instance, besides the *gdi* cutoff, we may require a minimum species split time (in generations or in years) (Rannala and Yang 2020). When there exist contact zones between populations, one may estimate the proportion of hybrids (*h*) (Anderson and Thompson 2002; Chakraborty and Rannala 2023), and contrast it with the historical migration rate (*m*) estimated from genomic data (Beerli 2006; Hey 2010; Hey et al. 2018; Gronau et al. 2011; Flouri et al. 2023). The rate ratio m/h may be used to measure reproductive isolation: a value of 1 means that introgressed alleles are neutral and have the same chance of being retained as a native allele in the recipient population, while $m/h \ll 1$ means that introgressed alleles are strongly deleterious and purged from the population

by natural selection, indicating the existence of (post-)zygotic reproductive isolation (Westram et al. 2022). A composite criterion incorporating m/h may be informative about species status, although a strict adherence to reproductive isolation (i.e., $m/h = 0$) as the criterion for delimiting species may be untenable given the prevalent nature of gene flow between well-recognized species.

While acknowledging the caveats of empirical species delimitation, we suggest that our pipeline allows one to utilize the power of the MSC framework and the *bpp* program to estimate population parameters precisely and accurately using the ever-increasing genomic sequence data. In particular, the recent implementation of the MSC-M model in *bpp*, having been applied to genome-scale datasets with thousands of loci (Flouri et al. 2023; Thawornwattana et al. 2022, 2023), has greatly improved the biological realism of models that are available for analyzing genomic data from closely related species and populations, the species status of which is yet to be determined. We hope that our pipeline may become a useful tool for evolutionary biologists to assess the genetic evidence for species delimitation, which should be integrated with other lines of evidence, including morphological and behavioral characteristics, and patterns of hybridization (Fujita et al. 2012; Solis-Lemus et al. 2015; Kim et al. 2022).

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SUPPLEMENTARY MATERIAL

Data available from the Dryad Digital Repository: <https://doi.org/10.5061/dryad.jm63xsjhc>.

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CONFLICT OF INTEREST

The authors declare that there is no conflict of interest.

DATA AVAILABILITY

The *hhsd* pipeline is written in python, and drives parameter estimation under the MSC or MSC-M models using *bpp*. The source code, documentation, and empirical datasets analyzed in the paper are available at <https://github.com/abacus-gene/hhsd>.

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